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Entanglement Relaxation of Poly(1-butene) and its Copolymer with Ethylene Detected in Conventional Shear Rheometer and Quartz Resonator

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Abstract:

This study examined linear viscoelasticity (LVE) of stereo-regular poly(1-butene) (PB) and its random copolymer with polyethylene (PBE), with number fraction of ethylene comonomer ≤ 10%, using a conventional shear rheometer combined with a quartz resonator. This combination resulted in the detection of LVE in a broad frequency range from Rouse region to terminal relaxation. LVE thus determined was fit to the double reptation model through utilizing inputting molecular weights determined by gel permeation chromatography equipped with refractive index and two-angle laser light scattering monitors, and the segmental time and entanglement molecular weight as the two fitting parameters. Quantitative prediction was finally achieved when the two fitting parameters changed systematically by the increase of ethylene content; a decrease of segmental time quantified a plasticizing effect and a decrease of entanglement molecular weight reflected enhanced chain flexibility. The entanglement molecular weight of the PB samples was found to be lower than those reported for stereo-irregular PB, suggesting the important effect of stereo-regularity on chain flexibility.

1. Introduction

Stereo-regular isotactic poly(1-butene) (PB) and its copolymers with ethylene (PBE) are widely used as feed pipe, owing to tolerance against wide temperature shifts, high yield stress, and strong chemical resistance. Commercially available PB and PBE are usually synthesized with the Ziegler-Natta catalysts. The crystallization temperature is usually much higher than that of glass transition when the ethylene content is less than 10%, which results in a narrow temperature window for measuring melt rheology. [1-3]

To address this problem, one pathway would reduce the stereo-regularity in order to suppress crystallization. For example, Graessley and coworkers synthesized atactic PB and PE copolymers by hydrogenating the monodispersed polybutadiene samples synthesized through anionic polymerization, thereby varying PB content from 0% to 100% by tuning a ratio between the 1,4 and 3,4 additions. They then examined the linear viscoelasticity (LVE) of these atactic samples with varied PE content from 1% to 85% [4-6] to determine the plateau moduli G_e and, accordingly, the entanglement molecular weight (M_e) of these samples from

$$M_e = \rho RT / G_e \qquad , \qquad (1)$$

where M_e was evaluated to be 13,500g/mol for pure PB and decreased systematically with the increase of PE fraction, owing to the enhancement of chain flexibility. In addition, Graessley and coworkers noted an important plasticizing effect of the ethylene comonomers. [4-6] Namely, T_g reduced with increased ethylene content. Nevertheless, it remains unclear how M_e and T_g change with stereo-regularity.

To gain more insight into this question, an alternative pathway involves extending the window of time scales of the LVE measurements. Toward this end, Friedrich and coworkers

recently demonstrated that the use of a conventional shear rheometer (detecting a frequency range of ~ 10^{-2}-10^2rad/s), a piezoelectric rotary vibrator (PRV, detecting a frequency range of ~ 1-10^4rad/s), and a quartz resonator (QR, detecting a frequency range of ~ 10^8rad/s) enables the detection of LVE from the Rouse regime to terminal relaxation for semi-crystalline PE and poly (vinyl acetate) (PVAc) copolymers. [7] This protocol is particularly useful when the ethylene content is above 60%, the point at which crystallization of PE disturbs conventional LVE measurements at low T, in turn, enabling QR to effectively extend LVE measurements to the glassy-to-rubbery transition region.

The present study will examine linear viscoelasticity for stereo-regular PB and PBE samples by combining conventional rheology and QR. [4-6; 8] Although this experimental approach is arguably very similar to that of Friedrich and coworkers, their work is extended herein by the addition of a new data analysis protocol. We utilized molecular weight (MW) and its distribution directly obtained from gel permeation chromatography equipped with refractive index and light scattering monitors as inputting parameters, leaving only entanglement molecular weight (M_e) and segmental time (τ_0) as the fitting parameters. This approach enables quantitative prediction of LVE. Comparison of the entanglement molecular weight M_e of stereo-regular PB in this study and that of stereo-irregular PB studied by Graessley and coworkers suggests the important role of stereo-regularity in determining the chain flexibility. [9]

2. Experimental

2.1 Samples

All PB and PBE samples were produced by LyondellBasell Industries with the brand name listed in Table 1. For simplicity, we renamed the samples based on the molecular weights and fraction of ethylene monomers, as also shown in Table 1; for example, PB0800 is renamed as PB121, meaning that this PB sample has M_w = 121kg/mol, and PB8510 is renamed as PBE203-9.9%, meaning that this PBE copolymer sample has M_w = 203kg/mol and a molar fraction of ethylene monomers f_{PE} = 9.9%. Most commercially available PBE samples contain high content of stereo-regular PB owing to their application values.

Tacticity of the three PB samples was characterized *via* ^{13}C nuclear magnetic resonance. Meso and racemic placements consisted of two adjacent monomers oriented in the same and opposite directions, respectively. ^{13}C enables characterization of fractions of isotactic (mm), heterotactic (mr or rm), and syndiotactic (rr) triads, with [mm] + [mr] + [rm] + [rr] = 1. Tacticity is defined as [m] = [mm] + 0.5([mr]+[rm]). Details of these parameters are summarized in Table 2.

Table 1. Important parameters of PB and PBE samples

Name	Code	f_{PE}	M_n(g/mol)	M_w(g/mol)	M_w/M_n	T_g^b(°C)	T_g^c(°C)
PB0800	PB121	0%	47,000	121,000	2.6	-26	-29
PB0400	PB238	0%	96,000	238,000	2.5	-25	-28
PB0110	PB742	0%	227,000	742,000	3.3	-22	-27
PB8640	PBE552-1.5%	1.5%^{a}	160,000	552,000	3.5	-27	-31
PB8220	PBE414-4.3%	4.3%^{a}	151,000	414,000	2.7	-32	-34.5
PB8510	PBE203-9.9%	9.9%^{a}	77,000	203,000	2.6	-35	-35.5

a: Reported in Ref [10; 11]

b: Obtained from the WLF analysis

c: Obtained from the DSC measurements of crystallized samples

Table 2: Tacticity of the PB samples

Name	Code	[mm]	[mr]+[rm]	[rr]	[m] (tacticity)
PB0800	PB121	0.960	0.020	0.020	0.970
PB0400	PB238	0.915	0.054	0.0311	0.942
PB0110	PB742	0.954	0.032	0.014	0.970

2.2 Gel Permeation chromatography (GPC)

Molecular weight distribution of PB and PBE samples was characterized by high-temperature gel permeation chromatography (HT-GPC) analysis with PL-GPC 220 (Agilent), and the instrument was equipped with a two-angle (15° and 90°) laser light scattering (TALLS) detector, a viscometer, and a differential refractive index (DRI) detector. Three PLgel 10 μm MIXED-B LS columns (300x7.5mm) were used for the separation.

The TALLS and the DRI detectors were calibrated with standard polystyrene (PS) samples. 1,2,4-trichlorobenzene stabilized with 5×10^{-4} g/mL 2,6-di-*tert*-butyl-4-methylphenol (BHT) was used as the eluent. All measurements were performed at 150°C with an eluent flow rate of 1.0 mL/min. Polymer solution at a concentration of about 1.0 mg/mL was injected into the multi-detector GPC system *via* an autosampler with an injection volume of 200 μL. The refractive index increment *dn/dc* of all studied PB and PBE samples was determined to be $-(0.097 \pm 0.001)$ mL/g.

Cirrus software was used for data acquisition and analysis. For each elution fraction i, the molecular weight M_i, radius of gyration $R_{g,i}$, intrinsic viscosity $[\eta]_i$, and concentration C_i

were obtained. Then the weight average and number average molecular weights, M_w and M_n, of the samples could be calculated with established absolute calibration curves, and results are summarized in Table 1.

2.3 DSC measurement

Thermal properties of the samples were measured with both conventional differential scanning (DSC) calorimeter (TA Instruments Q20) and Flash DSC. For conventional DSC measurements, specimens weighing 5-8mg, as cut from granules, were sealed in aluminum pans. The DSC equipment was calibrated using indium and tin. All experiments were performed under the protection of nitrogen atmosphere flowing at a rate of 50 mL/min.

To determine the glass transition of the crystallized sample, the samples were first annealed in the DSC instrument at 180°C for 10min (>> equilibrium crystallization point of 146°C of PB [29]) to remove thermal and flow histories, followed by cooling down to different temperature T_c and annealing there for 25min for isothermal crystallization ($T_c = 90°C$ for all PB samples, 70°C for PBE414-4.3% and PBE203-9.9%, and 40°C for PBE203-9.9%, at which the isothermal crystallization was finished within 25min). After isothermal crystallization, the samples were cooled down at a rate of 20°C/min to -80°C and then heated up to 20°C at a rate of 15°C/min. Glass transition T_g was determined by the DSC traces during the heating processes.

To understand the crystallization kinetics, all samples were subjected to fast scanning calorimetry (FSC) with Flash DSC (Mettler-Toledo Flash DSC 1) under the protection of nitrogen. The FSC sensor was conditioned and temperature-corrected according to the operating manual. The samples were microtomed into films, and the films were loaded on the

sensor and melted therein to ensure good contact with the sensor. During the measurements, the samples were first annealed at 180°C to remove the thermal and flow history, cooled down at different rates, and then heated up at a fixed rate of 1000°C/s, during which the crystals, if formed during the first cooling process, would melt, allowing calculation of the degree of crystallization by the resulting enthalpy (area integrated on the melting peak). This protocol was repeated by increasing the cooling rate until the sample could be effectively quenched and no melting peak could be detected in the heating process.

2.4 Conventional rheometry

Linear viscoelasticity (LVE) measurements were conducted on the MCR-302 (Anton Paar) and ARES-G2 (TA Instrument) with 25mm parallel plates. The samples were loaded at 180°C and annealed for 10min to remove thermal history. After that, frequency sweep measurements were conducted every 10-20°C from 180°C to lower T until the sample started to crystallize and G' increased with time at given T. During the frequency sweep measurements, strain amplitude was kept small ($\leq$10%) to ensure that the storage and loss moduli, G' and G'', were obtained within the linear regime as confirmed with the strain sweep measurements.

2.5 Quartz resonator

Our homemade quartz resonator is equipped with an AT-cut quartz crystal (14 mm in diameter, Hangzhou Longqin Advanced Materials Sci & Tech Co., Ltd., Hangzhou, China)

with gold electrodes (5 mm in diameter) on both sides, for which the basic frequency is 6 MHz, and could be extended to 3rd, 5th and 7th overtones.

Before measuring the sample, the bare quartz crystal was loaded on a homemade holder, and the holder was placed into an oven (V0 200, Memmert GmbH). After a two-hour equilibration at each testing T (= 115.3, 126.7, 150.5 and 160.0°C) in the oven, the resonance curve of bare quartz crystal was measured by using a quartz crystal microbalance based on admittance analysis (QCM-A DBY-17, Hangzhou Longqin Advanced Materials Sci & Tech Co., Ltd., Hangzhou, China) with a control program, "QCM-DBY". By fitting the quartz crystal resonance curves, the resonance frequency ω_0 and width at half-height D_0 of the resonance peak were determined at each basic frequency and overtone at each T. After that, a sample membrane with predetermined diameter (~ 5mm) and thickness (0.3mm), prepared with a homemade compressor, was loaded on the gold electrode at one side of the quartz crystal. The sample and the quartz crystal were placed back into the oven and heated to 160.0°C in vacuum. This process ensured that sample and quartz crystal would maintain good contact.

Next, the quartz crystal coated with sample was heated at each testing T in the oven for a two-hour equilibration. The resonance curve of the sample-coated quartz crystal was then measured again to give the resonance angular frequency ω and width at half-height D of the resonance peak at each basic frequency and overtone. Moduli were determined from shift of angular frequency $\Delta\omega = \omega - \omega_0$ and change of peak width, as $\Delta D = D - D_0$ (both in unit of rad/s), in the following equations:

$$G' = k(\Delta D^2/4 - \Delta\omega^2) \tag{2a}$$

$$G'' = -k\Delta D\Delta\omega \tag{2b}.$$

Here, $k = (d_q \rho_q)^2/\rho_p$ is a prefactor (Note that k is different by a factor of $4\pi^2$ from that reported in Ref [7] due to different units of frequency, i.e. rad/s here and Hz in Ref [7].), d_q and ρ_q are the thickness and density of quartz, respectively, and ρ_p is the density of the probing sample. From Eq. 2(a) and (b), we see that $\tan \delta = G''/G' = \Delta D \Delta \omega/(\Delta D^2/4 - \Delta \omega^2)$ is directly related to ΔD and $\Delta \omega$.

In the QR measurement, G' and G'' do not depend on membrane thickness as long as this membrane is sufficiently thick and fully covers one of the two gold electrodes. The penetration depth of acoustic shear wave generated by the quartz resonator in a viscoelastic liquid p is given as $p = (2\eta/\omega\rho)^{1/2} = (2G/\omega^2\rho)^{1/2}$, where ρ is the density of the viscoelastic liquid, and η and G are viscosity and shear modulus of the viscoelastic liquid, respectively. [12] The largest penetration depth p of the shear wave can then be estimated to be about 37.5 μm by taking ρ of 1.0 g/cm^3 and G of 1GPa as the fundamental frequency of the quartz resonator at 6 MHz, which is far smaller than the thickness of sample, i.e., ~0.3mm. For higher 3rd, 5th and 7th overtones, the penetration depths are even smaller. In such cases, the quartz resonator senses the only a thin layer of the bulk sample in melt state.

3. Theory

The modulus is expressed as a sum of the Rouse part, G_R, and reptation part, G_{rep}, as

$$G(t) = G_{Rouse}(t) + G_{rep}(t) \tag{3}.$$

The Rouse part can be written as

$$G_{\text{Rouse}}(t) = G_e \sum_N \frac{N_e}{N} \phi(N) \left\{ \frac{1}{5} \sum_{q=1}^{N/N_e} \exp\left(\frac{-tq^2}{\tau_e (N/N_e)^2} \right) + \sum_{N/N_e+1}^{N} \exp\left(\frac{-tq^2}{\tau_e (N/N_e)^2} \right) \right\}$$

(4).

Here, G_{Rouse} contains two types of relaxation modes. The first term in the brace corresponds to low-order motional modes of length scales larger than the entanglement length, and the second term corresponds to the high-order motional modes corresponding to length scales smaller than the entanglement length. For the first term, a prefactor of 1/5 is added, as derived by Likhtman and McLeish. [13]

The reptation part of modulus, on the other hand, can be expressed in the double reptation model [14-17] as

$$G_{\text{rep}}(t) = G_e \left(\sum_N \phi(N) F(t,N) \right)^2,$$

(5)

where a power 2 reasonably accounts for the constraint release mechanism. $F(t,N)$ is expressed in a form by

$$F(t) = \frac{8}{\pi^2} \sum_{\text{odd } q} \frac{1}{q^2} \exp\left[-q^2 U(t) \right] \quad,$$

(6a)

with $\quad U(t) = \frac{t}{\tau_{\text{rep}}} + \frac{\beta M_e}{M} g\left[\frac{tM}{\tau_{\text{rep}} \beta M_e} \right]$ and $g(x) = \sum_{m=1}^{\infty} \frac{1 - \exp(-m^2 x)}{m^2}$

(6b)

4. Results and discussion

4.1 Molecular weight distribution

The static light scattering detector monitors the Rayleigh ratio $R_{\theta,i}$ of the i-th fraction, which

is related to the fraction concentration C_i as

$$\frac{KC_i}{R_{\theta,i}} = \frac{1}{P(\theta)_i\, M_{w,i}} + 2A_{2,i}C_i + ... \tag{7}$$

where the second and higher-order terms of C_i can be ignored for dilute concentration

employed in the GPC measurements. Rayleigh ratios at two angles of the TALLS detector,

$\theta_1 = 15°$ and $\theta_2 = 90°$, enable calculation of their ratio $Z_i = R_{\theta1,i}/R_{\theta2,i} = P(\theta_1)_i/P(\theta_2)_i$.

Accordingly, the radius of gyration R_{gi} and the particle scattering function $P(\theta_1)_i$ of the i-th

fraction can be obtained from the ratio Z_i by the built-in Cirrus software with the random coil

assumption for the particle scattering function. Then, the molecular weight M_i of the fraction

is calculated with the known concentration from the DRI detector. [18; 19]

Figure 1 shows plots of M as functions of the elution volume V for all PB and PBE samples

in this study. The difference among samples is trivial based on the similarity of their

chemical structures. Scattering of data points is noted at both ends of the chromatograms

since $M_{w,i}$ is, in principle, calculated from a ratio of the LS and RI signals that are

proportional to $C_iM_{w,i}$ and C_i, respectively, and, thus, errors would appear when either of the

signals approaches zero. To solve this data scattering problem, we use linear fit of the $\log M -$

V plots at medium V where the scattering is sufficiently small (R^2 value ≥ 0.997) and

extrapolate the line to the high and low ends of elution volumes. This linear assumption of

the calibration curves should hold for the samples in this study because the employed PLgel

10μm MIXED-B LS GPC columns have a linear molecular weight range of 500-10,000,000

g/mol.
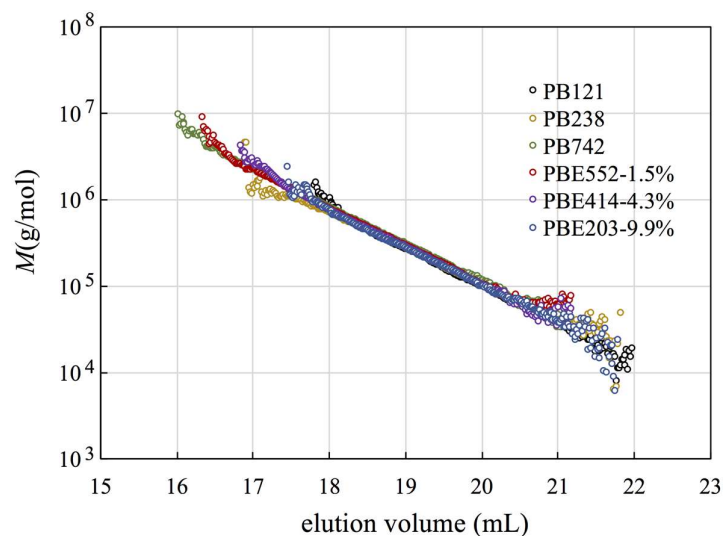
Figure 1: Molecular weight M as a function of elution volume V for all PB and PBE samples obtained by the multi-detector GPC.

With the absolute calibration curve of each sample established, the molecular weight distributions of the PB and PBE samples can be obtained, and the results are shown in Figure 2. The overall trend is a broadening of the molecular weight distribution with increasing molecular weight, as demonstrated in the plots and the M_w/M_n values listed in Table 1, which should be related to the detailed synthesis procedure that is unknown to us.
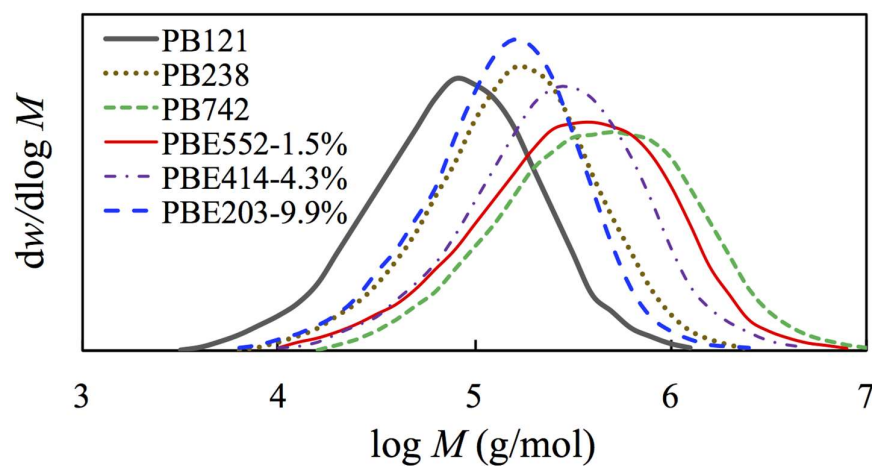

Figure 2: Molecular weight distributions of PB and PBE samples.

4.2 Linear viscoelasticity

Figure 3 shows the storage and loss moduli, G' and G'', measured as functions of angular frequency ω for all PB and PBE samples reduced at a reference $T_r = 120°C$. The moduli are multiplied by an intensity factor, $b_T = T_r/T$, and shifted horizontally to construct the master curves. In principle, the modulus having entropic origin should be proportional to ρT, and a normalization factor should be $\rho_r T_r/\rho T$. Nevertheless, a change of ρ is usually much weaker than T itself; therefore, we ignore the change of ρ in our analysis. Time-temperature superposition can be achieved very well for the low ω $b_T G'$ and $b_T G''$ data measured from conventional rheometry, for which the uncertainty of each data point is usually less than $\pm$ 5%, corresponding to ± 0.02 in the logarithmic scale, i.e., the size of symbols. In comparison, a similar quality of data cannot be achieved for the high ω $b_T G'$ and $b_T G''$ data detected in QR, which shows the scattering data quite clearly. For these data, it is difficult to shift the QR data precisely up to ~ 0.02 in logarithmic scale along the horizontal axis. Therefore, we shifted the data under the guidance of low ω LVE data by conventional rheometry. That is, we shifted the QR data detected at 115.3, 126.7, 150.5 and 160.0°C by interpolating points of the plots of a_T against T of conventional rheometry, assuming that high and low ω data exhibit the same temperature dependence. Since the temperature range of QR measurements is well within that of conventional rheological measurements, this protocol should be acceptable. The shift factors of LVE data by conventional rheometry and the interpolation points of QR are summarized in Figure 4 (a). The master curves thus constructed are further shifted by a vertical factor A, as indicated (larger A is chosen for higher M sample), to avoid overlapping.

The solid curves in Figure 3 are predicted on the basis of the double reptation model by utilizing density $\rho = 0.813$g/cm^3, as reported by Graessley. [20] The temperature for this reported density is 140°C, very close to $T_r = 120$°C in this study. The fitting parameters are summarized in Table 3, including a fixed shape parameter β (fixed to be $\beta = 9$, identical to $\beta = 9$ reported for poly(vinyl ethylene) [21] and close to $\beta = 8.7$ reported for polystyrene [15]), entanglement molecular weight M_e and Rouse time per Kuhn segment τ_0. We first determined this factor β through fitting LVE of pure PB and utilized the same factor for all the samples. Since a fixed β enables us to achieve good predictions, we did not intend to introduce one additional adjustable parameter. The molecular weight per Kuhn segment is $M_K = 133$g/mol for PB, which is assumed to be the same for the PBE samples. This assumption is innocuous here since (1) a fraction of PE is low ($f_{PE} < 10\%$) and (2) all LVE studied here are below $G_K = \rho RT/M_K = 2 \times 10^7$Pa. Thus, while the choice of M_K would affect τ_0, it would not affect predictive quality. In the model calculation, a power region $G' = G_K(\omega\tau_0)^{1/2}$ can be used to guide the choice of τ_0. The molecular weight distribution $\phi(N)$ with $N = M/M_0$ in Eq. 5 was shown earlier in Figure 2. By utilizing M_e as a fitting paraemeter, we can calculate entanglement time $\tau_e = \tau_0(M_e/M_0)^2$ and reptation time $\tau_{rep} = \tau_e(M/M_e)^3$ in Eqs. 3-6. These parameters enable quantitative prediction of LVE in the frequency range of our measurements based on the double reptation model.

In Appendix B, we fit LVE based on the hierarchical model by Wang et al. by utilizing the same M distribution and τ_0, as shown in Figure 3, and M_e as the fitting parameters. [22] Good agreement could also be achieved between the experimental results and the theoretical prediction (cf. Figure B1).

Since the calculations, as expressed in Eqs. 3-6, consider only the rubbery part of modulus, the predicted glassy-to-rubbery transition is characterized by $G' = G'' \sim \omega^{1/2}$ that ends at high ω where G' (= G_K) becomes higher than G''. In contrast to this expectation, it is clear that G'' is higher than G' at the high ω end. This feature indicates that the glassy part of G'' starts to play a role at the high frequency end of the glassy-to-rubbery transition region, as observed extensively in the rheo-optical measurements performed by Inoue and coworkers. [23; 24] To address the contribution of glassy modulus, [23-25] we added $G_{glassy}'' = \eta_{glassy}\omega$ to the rubbery part of G'', where $\eta_{glassy} = 0.045$Pa.s chosen to be the same for all the samples. This step leads to $G'' > G'$ at high frequency (see the dashed curves), which agrees with the experimental results. We should note that the glass modulus can be represented in more precise ways. For example, Marin and coworkers have suggested that the complex G_{glassy}^* can be represented as $G_{glassy}(\omega) = G_{inf} - G_{inf}/(1+i\omega\tau_{glassy})^{1/2}$, or in time domain as $G_{HF}(t) = G_{inf}(1-\mathrm{erf}(t/\tau_{glassy})^{1/2})$. [26; 27] An alternative representation is the Kohlrausch-William-Watts (KWW) equation $G_{glassy}(t) = G_{inf}\exp(-t/\tau_{glassy})^{\beta})$. [28-30] Since both the models above would give $G_{glassy}'' = \eta_{glassy}\omega$ and $G_{glassy}'' > G_{glassy}'$ in the glassy-to-rubbery transition region of current interest, we may safely use $G_{glassy}'' = \eta_{glassy}\omega$ here as an approximation.
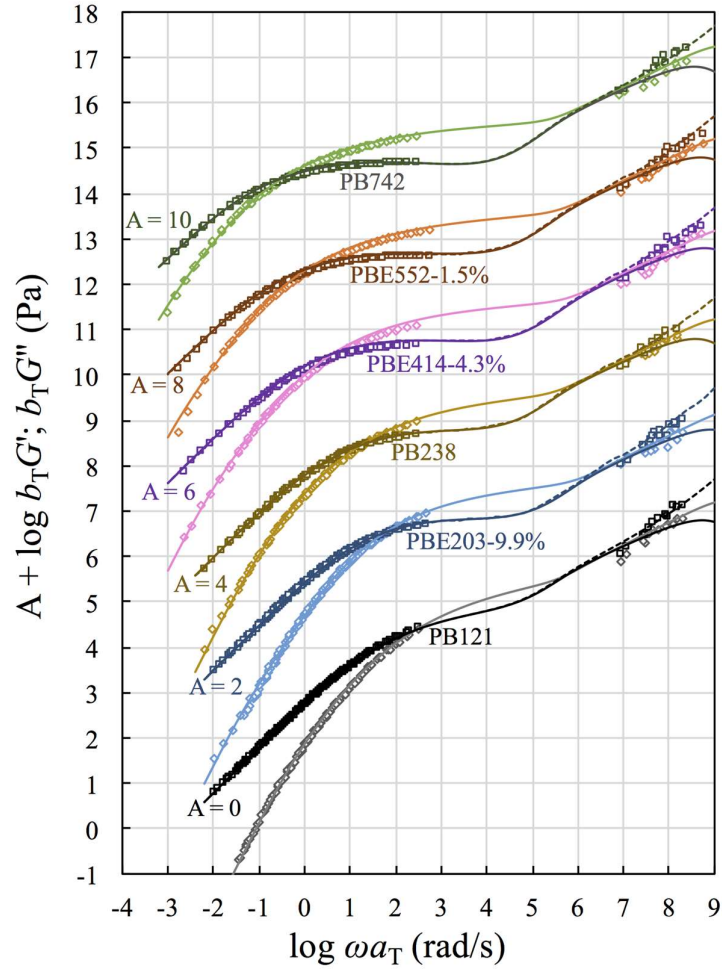
Figure 3: Comparison of LVE master curves (symbols) of storage and loss modulus, G' and G'', measured as a function of angular frequency ω and reduced at reference temperature $T_r =$ 120°C for the PB and PBE samples and prediction (curves) of the double reptation model. The LVE data are shifted along the vertical axis by a factor of A as indicated, where larger A was chosen for higher M sample.

Table 3. Inputting parameters for model calculation at reference $T_r = 120$°C

Brand Name	Code	M_e(g/mol)	τ_0(ns)	β

PB0800	PB121	7,500	0.66	9
PB0400	PB238	7,000	0.93	9
PB0110	PB742	7,500	1.0	9
PB8640	PBE552-1.5%	7,500	0.63	9
PB8220	PBE414-4.3%	6,700	0.59	9
PB8510	PBE203-9.9%	6,300	0.43	9

4.3 Effective glass transition temperature and segmental time

The shift factors a_T of the PB and PBE samples are plotted against T in Figure 4 (a). The temperature dependencies do not agree well, suggesting that T_g is different for these samples. Graessley and coworkers analyzed the viscoelastic shift factors of random PBE samples obtained through hydrogenating monodispersed polybutadiene samples of different ratios of 1,4 and 3,4 additions. They found that an empirical Williams–Landel–Ferry (WLF) equation holds for all PBE samples having various PB and PE ratios [4-6], as

$$\log a_{\mathrm{T}} = \frac{-6.35\left(T - T_g - 77\right)}{146 + \left(T - T_g - 77\right)} \tag{8}.$$

By choosing an iso-frictional temperature $T_{\mathrm{iso}} = T_g + 77$, as the reference temperature, we can rewrite Eq. 8 as $\log a_{\mathrm{T}} = -6.35(T - T_{\mathrm{iso}})/(146 + T - T_{\mathrm{iso}})$, as shown in curve in Figure 4(b). By taking T_{iso} as an adjustable parameter, we check the consistency between the plots of $\log a_{\mathrm{iso}} = \log a_{\mathrm{T}}(T_r) - 6.35(T_r - T_{\mathrm{iso}})/(146 + T_r - T_{\mathrm{iso}})$ against $T - T_{\mathrm{iso}}$ (symbols in Figure 4(b)) and the prediction by Eq. 8 (curve in Figure 4(b)) until the best agreement can be achieved. The scattering of data points is effectively reduced compared with those in Figure 4(a). From the

fitting parameter T_{iso} thus determined, we can further calculate the effective T_g as $T_g = T_{iso} - 77$, which is summarized in Table 1 and will be compared with the DSC T_g later in Figure 5.
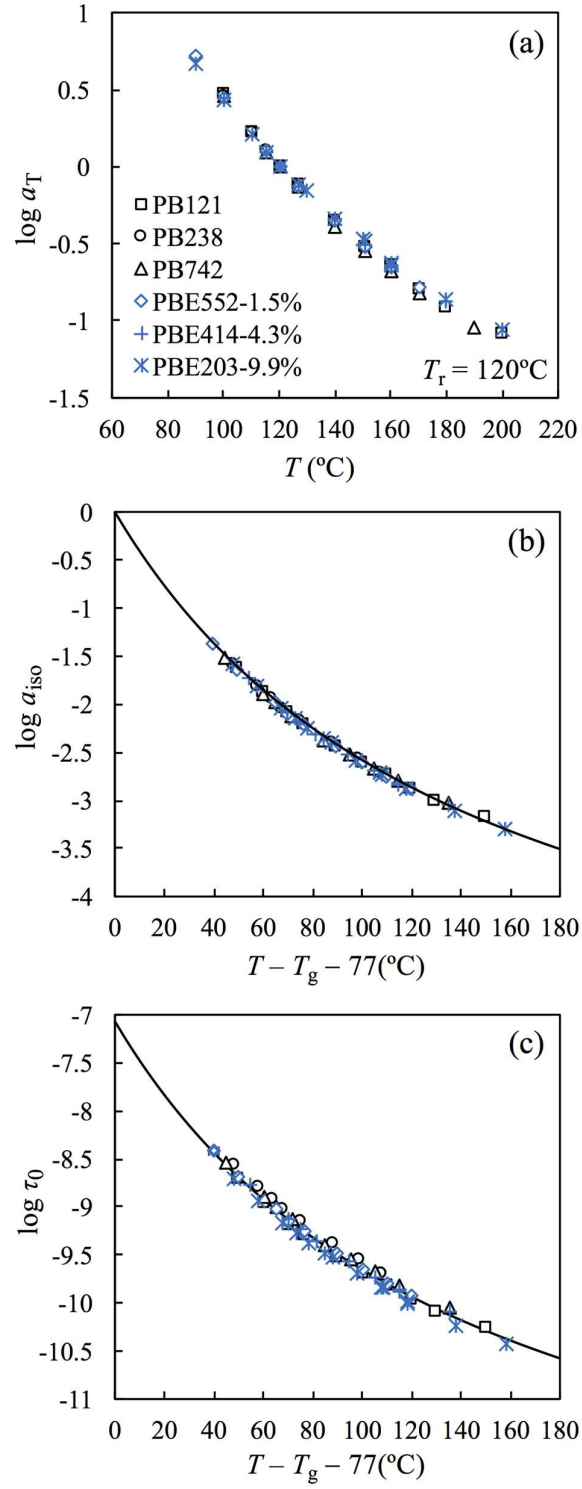
Figure 4: Comparison of (a) viscoelastic shift factor a_T against T for the PB and PBE samples, with reference temperature $T_r = 120°C$, (b) viscoelastic shift factor a_{iso} reduced to an iso-frictional temperature $(T - T_g -77)°C$ when a_{iso} shows the same temperature dependence and can be fit by WLF Eq. 8, and (c) segmental time τ_0 reduced to $(T - T_g -77)°C$.

Since the samples are reduced at an iso-frictional state at $(T - T_g - 77)$ °C (Figure 4(b)), it can be expected that the segmental time can be properly normalized at $(T - T_g - 77)$ °C. This expectation is tested in Figure 4 (c), showing that the segmental time τ_0 extracted from the analysis of LVE at T_r (in Figure 3) is extended to another T through the viscoelastic shift factor a_T and plotted against $(T - T_g - 77)°C$ (i.e., $T - T_{iso}$). It is remarkable that the plots of τ_0 against $(T - T_g - 77)°C$ agree for all PB and PBE samples. The solid curve is defined by [4]

$$\log \tau_0 = -7.07 - \frac{6.35\left(T - T_g - 77\right)}{146 + T - T_g - 77} \tag{9}$$

which is a reasonable representation of τ_0 obtained for all the PB and PBE samples in this study, as $\log \tau_0 = -7.07$ at $T = (T_g + 77)°C$.

Figure 5 compares T_g plotted against the fraction of PE from our WLF analysis (filled diamonds) and that by Graessley and coworkers (filled spheres), both representing T_g of the samples in melt, [4] and T_g measured directly from DSC by us (unfilled diamonds) and by De Rosa et al. (unfilled squares), both representing T_g of the semi-crystallized samples. [31] It is worth mentioning that the samples studied by De Rosa et al. are stereo-regular samples synthesized with the zirconocene catalyst. Difference is revealed from comparing T_g from the WLF analysis (filled diamonds) and that from the DSC measurements (unfilled diamonds) in this study, which is not surprising because the former is given on the melt samples while the latter is on the amorphous phase of the semi-crystallized samples. This difference becomes

smaller for the PBE203-9.9% sample possibly because it has the lowest degree of crystallization owing to the highest content of PE. Although the difference exists, the overall trend is similar in that T_g decreases with increasing fraction of ethylene (f_{PE}) comonomers.

The dashed curve corresponds to the prediction of the empirical Fox equation: [32]

$$T_g = \frac{f_{PE}}{T_{g,PE}} + \frac{1 - f_{PE}}{T_{g,PB}}$$

(10)

which underestimates the plasticizing effect of PE. In comparison, the empirical DiMarzio equation with one additional fitting parameter, $r = 0.81$, can give better prediction: [33]

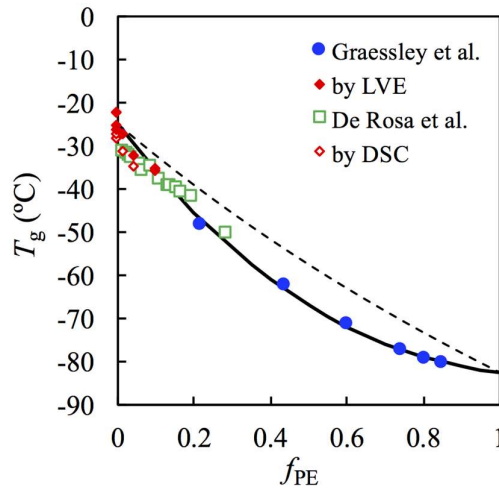$$T_g = \frac{f_{PE} T_{g,PE} + r(1 - f_{PE}) T_{g,PB}}{f_{PE} + r(1 - f_{PE})}$$

(11).

Figure 5: Comparison of effective glass transition temperature T_g against a number fraction of ethylene monomers. The filled spherical symbols are data reported by Graessley and coworkers, and the unfilled square symbols are data of De Rosa et al, and filled and unfilled diamond symbols are data in this study. The solid and dashed curves correspond to predictions using the DiMarzio and Fox equations, respectively.

4.4 Entanglement molecular weight

Figure 6 compares the entanglement molecular weights (M_e) of PB and PBE samples obtained from fitting the data to the double reptation model (square symbols) and the hierarchical model of Larson and coworkers (diamond symbols, cf. Appendix B for details), as well as that calculated from G_e reported by Graessley and coworkers (spherical symbols). [4] The overall trend is a decrease of M_e with increasing fraction of PE, reflecting higher chain flexibility for samples with higher f_{PE}. The entanglement spacing of isotactic PB in this study is smaller than that of the atactic PB sample studied by Graessley and coworkers, as discussed below. [4]

One of the simplest rules that correlates the molecular weight per backbone and M_e is the "backbone equivalence" model. In this model, the size of a coil is assumed to be determined by the backbone PE so as to give the packing length $p \sim m_b$. Since the entanglement length is proportional to the packing length as $a = P_e p$, with $P_e \sim 20$ appearing to be a constant, the volume per entanglement segment becomes $M_e/\rho = a^2 p = P_e^2 p^3 \sim m_b^3$. A difference of the density ρ of different polyolefins could be ignored to give [8; 34]

$$M_e = M_{e,PE}(m_b/m_{b,PE})^3 \tag{12}$$

where $M_{e,PE} = 1,000$g/mol and $m_{b,PE} = 14$g/mol are the molecular weights per entanglement and per backbone of PE, respectively. This equation was derived earlier by Fetters, Lohse and coworkers (c.f. Eq. 13d of ref [34]). The backbone equivalence assumption can be interpreted as a constant ratio between trans/gauche conformational isomers (conformers). However, it is well known that this ratio changes according to the length and arrangements of

the side chains, i.e., monomer type and the tacticity. Taking these factors into consideration, the simplest adaptation would use the power in Eq. 12 as a fitting parameter to give

$$M_e = M_{e,PE}(m_b/m_{b,PE})^{\alpha} \tag{13}$$

where α reflects the roles of monomer chemistry and tacticity. Figure 6 compares M_e obtained for the heterotactic PB and PBE copolymers studied by Graessley and coworkers (blue spheres) and M_e obtained through fitting with the double reptation model (black squares) and hierarchical model (green diamonds). The solid and dashed lines correspond to the predictions of Eq. 13 with $\alpha = 3.3$ and 4.2, respectively. The different α values suggest the important role played by tacticity.

Fetters, Lohse and coworkers compared a prediction of Eq. 13 with experimental results of *more than ten different types of polyolefins* and concluded that the plateau modulus $G_N \sim m_b^{-3.49}$ for $m_b = 14\text{-}28\text{g/mol}$ and $G_N \sim m_b^{-1.58}$ for $m_b = 35\text{-}56\text{g/mol}$, corresponding to $M_e \sim m_b^{3.49}$ (for $m_b = 14\text{-}28\text{g/mol}$) and $M_e \sim m_b^{1.58}$ (for $m_b = 35\text{-}56\text{g/mol}$) if the difference of ρ is negligible. [34] Meanwhile, they observed $<R^2>/M \sim m_b^{-1.43}$ at 298K and $<R^2>/M \sim m_b^{-1.30}$ at 373/463K for $m_b = 14\text{-}28\text{g/mol}$, both stronger than $<R^2>/M \sim m_b^{-1}$ expected from the backbone equivalence model, which they attributed to an enhanced ratio of gauche conformers with m_b by the presence of branching groups. The higher $M_e \sim m_b^{3.49}$ compared to $M_e \sim m_b^3$, as predicted by the backbone equivalence model, should somehow be related to this enhancement. The solid and dashed curves in Figure 6 represent the prediction of Eq. 13 with $\alpha = 3.3$ and 4.1, respectively, where the former value is close to 3.49 reported by Fetters, Lohse and coworkers.

The solid curve with $\alpha = 3.3$ gives $M_e = 8,000$ for $f_{PE} = 0$, much smaller than $M_e = 13,500$, as determined from G_e reported by Graessley and coworkers. We suspect that this difference

results from a difference in stereo-regularity. For the isotactic PB and PBE samples in this study, a ratio between trans and gauche conformers should be more similar to that of PE, giving a value of $\alpha = 3.3$ close to a factor of 3 (that assumes this ratio to be unchanged). In contrast, for the heterotactic PB and PBE studied by Graessley and coworkers, the deviation of α becomes more prominent with increasing fraction of PB where $\alpha = 4.1$ (dashed curve) is required to predict the behavior of the pure PB sample, possibly related to a lack of tacticity that leads to a change of the trans/gauche ratio.
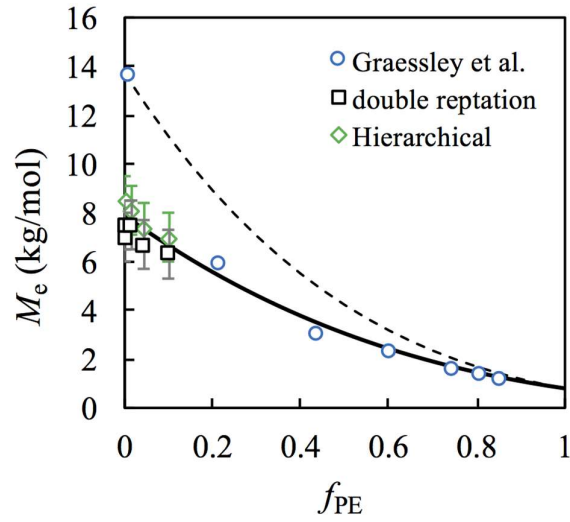

Figure 6: Comparison of M_e plotted against a number fraction of ethylene monomers of the PB and PBE samples. An error bar of ± 1000 is estimated for M_e from data fitting. The spherical symbols are calculated from G_e reported by Graessley and coworkers, and the square and diamond symbols are obtained through fitting with the double reptation and hierarchical models, respectively. The solid and dash curves correspond to the prediction of Eq. 13 with $\alpha = 3.3$ and 4.1, respectively.

5. Conclusion

This study explored the possibility of measuring the linear viscoelasticity of isotatic PB and PBE by using conventional rheometry in combination with the quartz resonator. The protocol of experiment and data analysis should be applicable to all semicrystalline polyolefins in melt.

The linear viscoelasticity from the Rouse to terminal relaxation could be detected above the crystallization temperature, which was further analyzed with the double reptation model. Such analysis enabled us to determine glass transition temperature T_g and entanglement molecular weight (M_e) of these samples.

Comparison of T_g and M_e with those parameters for atactic PB and PBE, studied by Graessley and coworkers, revealed the effects of stereo-regularity. The dependence of T_g on PE content seems to be consistent between isotactic and atactic samples. However, M_e is considerably larger for the atactic sample than the isotactic sample, suggesting the important role that stereo-regularity plays in chain flexibility.

Appendix A: Thermal analysis

Thermal measurements were conducted with both conventional DSC equipment Q20 (TA Instruments) and Flash DSC (METTLER TOLEDO Flash DSC 1). Conventional DSC equipment was used to characterize the glass transition temperature T_g of the semi-crystallized samples, to be compared with that reported by De Rosa et al. on isotactic PBE copolymers synthesized with the zirconocene catalyst, [31] while Flash DSC was employed to understand the minimum cooling rate required to effectively quench the samples without crystallization. Understanding this criterion helps in evaluating if the LVE of these samples

can be characterized through quenching the amorphous sample to a testing temperature without crystallization, a method that has been suggested by Kapnistos and Vlassopoulos. [35]

For the conventional DSC measurements, the samples were first annealed at 180°C for 10min to remove the thermal and flow histories and then subjected to isothermal crystallization. After that, the samples were cooled down at a rate of 20°C/min to -80°C and then heated to 20°C at a rate of 15°C/min, during which the DSC traces were recorded and shown in Figure A1. The DSC traces of PB238, PB742, PBE552-1.5%, PBE414-4.3%, and PBE203-9.9% were reported in our previous study, while the DCS trace of PB121 was only reported in this study. [36]

In Figure A1, the glass transition region becomes more prominent with increasing PE content because the introduction of ethylene reduces stereo-regularity and suppresses crystallization, leading to larger fraction of the amorphous phase that activates the stronger glass transition process. The glass transition temperature is chosen as the mid-point of the glass transition process, which increases slightly with increasing molecular weight owing to the well-known high free volume contribution of the chain ends, but decreases with increasing PE content, owing to the plasticizing effect of PE, which is similar to the trend reported in literature. [4; 37]
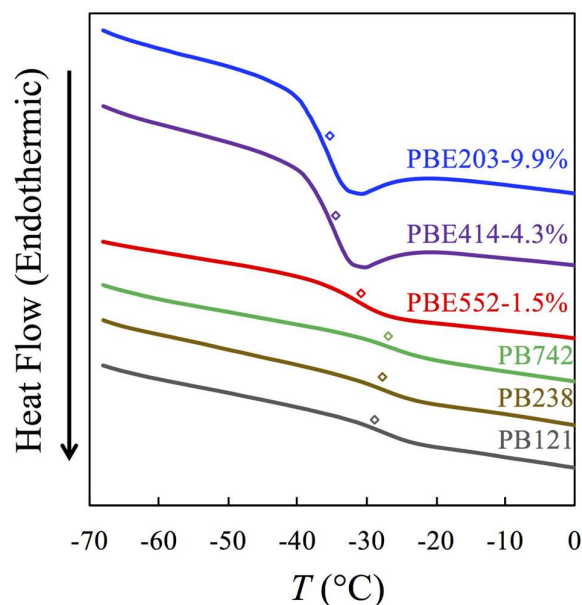
Figure A1: DSC traces of PB and PBE samples obtained after isothermal crystallization at different T_c.

Figure A2 shows the fast scanning calorimetry (FSC) traces detected at a heating rate of 1000°C/s after cooling down at different rates, as indicated. It can be seen that the threshold quenching rate to prevent crystallization is very high for the pure PB samples (top panels), i.e., 30°C/s for the PB121 and PB238 samples and 100°C/s for the PB742 sample. The threshold quenching rate gradually decreases for samples with higher content of ethylene comonomers by the suppression of crystallization kinetics after reducing stereo-regularity. From the bottom panels of Figure A2, we see that the threshold rates are 5°C/s for the PBE552-1.5% sample and 0.5°C/s (30°C/min) for the PBE414-4.3% and PBE203-9.9% samples. The latter value is close to the limited quenching rate of conventional rheometers. In addition, the quenching efficiency could be lower for the rheometers compared with the Flash DSC on the thinner sample membrane; therefore, we did not attempt to measure LVE of the effectively quenched samples.
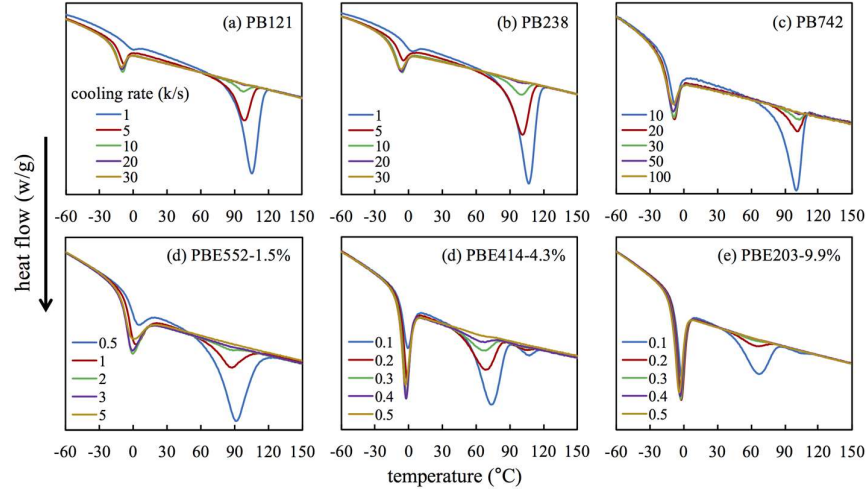
Figure A2: FSC traces recorded during heating at a rate of 1000°C/s after quenching the PB and PBE samples at different rates, as indicated.

Appendix B: Prediction of Hierarchical Model

We compared the experimental results with theoretical predictions made by using the Hierarchical-3.0 Model [22]. The hierarchical model is a tube-based computational model originally developed by Larson (Hierarchical-1.0) [38] for predicting the linear viscoelasticity (LVE) of general mixtures of entangled linear and branched polymers. This model was later refined by Park et al. (Hierarchical-2.0) [39] and Wang *et al.* (Hierarchical-3.0), "which incorporates several refinements of the relaxation mechanisms and also shows a higher computational efficiency due to the use of a logarithmic time stepping method for calculating the time evolution of the arm-end retraction", as explained in the context of the present work below (Wang et al., 2010). [22] The general theoretical framework of the hierarchical model

is based on the Milner-McLeish theory for blends of monodisperse star and linear polymers [40-42]

In the Milner-McLeish theories [40; 41] and, hence, the hierarchical model, entangled linear polymers are treated as symmetric two-arm stars with the arm-free ends retracting along the confining tubes of the polymers owing to contour length fluctuations until reptation takes over. For polydisperse polymer systems, constraint release (CR) effects are addressed by the dynamic tube dilation (DTD) theory. [43; 44] In addition, upon a sudden drop in the volume fraction of unrelaxed materials ($\Phi(t)$) in the system such that the DTD picture fails, relaxation enters a CR-Rouse regime whereby arm retraction occurs in a partially dilated tube, and the tube itself undergoes Rouse motion inside a wider supertube [41; 42; 45]. In the current work, we assume that the diameter of the partially dilated tube is determined by the unrelaxed volume fraction just before the onset time of the CR-Rouse regime, which is termed as the "thin" tube approach [22; 46]. The diameter of the supertube is determined by a supertube volume fraction which decreases with time in a power law, as $\Phi_{ST}(t) \sim t^{-1/2\vartheta}$, where ϑ is the dilution exponent. The CR-Rouse regime ends when $\Phi_{ST}(t)$ reaches the unrelaxed volume fraction $\Phi(t)$. In a highly polydisperse system, the process of entering and exiting the CR-Rouse regime may take place many times before the stress relaxation of the entire system is terminated by the reptation of the longest chains.

The influence of different relaxation mechanisms, numerical implementation methods, and choice of certain model parameters on the LVE predictions of the hierarchical model and another tube-based computational model, the "bob" (or branch-on-branch) model [46], has been discussed in detail in a previous publication [22]. For the entangled linear polymer systems studied in this work, the only variable model parameter is the dilution exponent ϑ which can be chosen as either 1 or 4/3. It has been shown in theoretical [47; 48] and

hierarchical model [22] calculations that the use of $\vartheta = 1$ can provide better predictions for the viscoelastic properties of binary blends of linear polymers than $\vartheta = 4/3$, which, however, works better for star-linear blends. The same trend has been found for the description of polydisperse linear PB and PBE melts. Therefore, all hierarchical model predictions presented here are generated using $\vartheta = 1$.

The input system parameters for the hierarchical model calculations include the plateau modulus

$$G_N^0 = G_e = \frac{\rho R T}{M_e} \tag{B1}$$

and the equilibration or entanglement time

$$\tau_e = \tau_0 \left(\frac{M_e}{M_0}\right)^2 \tag{B2}$$

where the same density and molar weight of monomers, $\rho = 0.813 \text{g/cm}^3$ and $M_0 (= M_k) = 133 \text{g/mol}$, are used for all studied samples. The reference temperature is set as $T = 120°C$. Both M_e and τ_0 for different PB and PBE samples are summarized in Table B1. The experimentally determined molecular weight distributions, as shown in Figure 2, are also used directly in the model calculations.

In Figure B1, the hierarchical model predictions for the LVE of different PB and PBE samples are shown to be in reasonably good agreement with the experimental data. The slightly higher theoretical values in the terminal relaxation regime (lowest frequencies) can be attributed to the artificially extended CR-Rouse regime whereby arm retraction in the "thin" tube leads to a faster decay of the unrelaxed volume fraction Φ compared to that of supertube volume fraction Φ_{ST} and, as such, results in an overestimation of the stress moduli [22]. This problem is most severe in describing star-linear blends with very low volume fractions of star polymers, but relatively innocuous for the polydisperse linear polymer systems studied here,

though still noticeable. The overestimation problem could be partly resolved by taking into account the disentanglement relaxation mechanism, which effectively cuts off the artificially extended CR-Rouse regime. [22; 38; 39]

Table B1. Inputting parameters for hierarchical model calculation at reference temperature T_r = 120°C

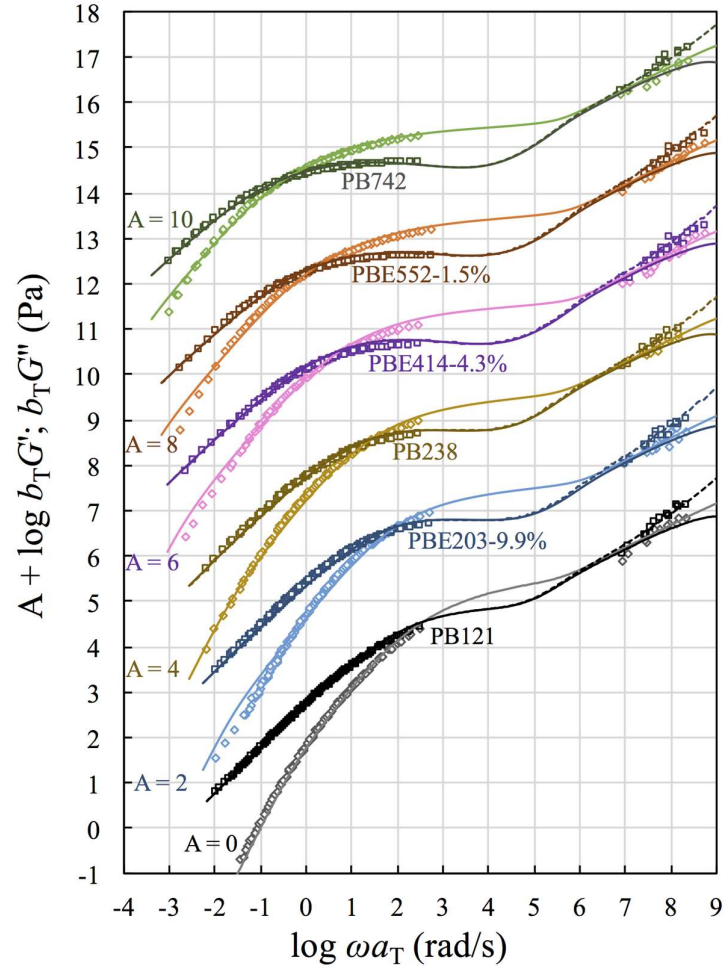| Brand Name	Code	M_e(g/mol)	τ_0(ns)
PB0800	PB121	7,500	0.66
PB0400	PB238	7,500	0.93
PB0110	PB742	8,500	1.0
PB8640	PBE552-1.5%	8,100	0.63
PB8220	PBE414-4.3%	7,400	0.59
PB8510	PBE203-9.9%	7,000	0.43

Figure B1: Comparison of LVE master curves (symbols) of storage and modulus, G' and G'', measured as a function of angular frequency ω and reduced at reference temperature $T_r = 120°C$ for the PB and PBE samples and prediction of the hierarchical model. The LVE data are shifted along the vertical axis by a factor of A, as indicated, where larger A was chosen for higher M sample.

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