

Stylized facts of intraday precious metals

Article

Published Version

Creative Commons: Attribution-Noncommercial-No Derivative Works 4.0

Open access

Batten, J., Lucey, B., McGroarty, F., Peat, M. and Urquhart, A. ORCID: https://orcid.org/0000-0001-8834-4243 (2017) Stylized facts of intraday precious metals. PLoS ONE, 12 (4). ISSN 1932-6203 doi: https://doi.org/10.1371/journal.pone.0174232 Available at https://centaur.reading.ac.uk/79175/

It is advisable to refer to the publisher's version if you intend to cite from the work. See <u>Guidance on citing</u>.

To link to this article DOI: http://dx.doi.org/10.1371/journal.pone.0174232

Publisher: Public Library of Science

All outputs in CentAUR are protected by Intellectual Property Rights law, including copyright law. Copyright and IPR is retained by the creators or other copyright holders. Terms and conditions for use of this material are defined in the <u>End User Agreement</u>.

www.reading.ac.uk/centaur

CentAUR

Central Archive at the University of Reading

Reading's research outputs online



Citation: Batten J, Lucey B, McGroarty F, Peat M, Urquhart A (2017) Stylized facts of intraday precious metals. PLoS ONE 12(4): e0174232. https://doi.org/10.1371/journal.pone.0174232

Editor: Wei-Xing Zhou, East China University of Science and Technology, CHINA

Received: November 16, 2016

Accepted: March 5, 2017

Published: April 27, 2017

Copyright: © 2017 Batten et al. This is an open access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

Data Availability Statement: All data are fully described in the paper and are available from a commercial source, Thomson Reuters Tick History Database. This is however a subscription database. Readers may contact Thomson Reuters Tick History Database at the following link to access the data in the same manner by which the authors obtained it: https://customers.reuters.com/rph/trth/ sliver.aspx?section=ContactUs. On request to Maurice Peat, readers may request the data (maurice.peat@sydney.edu.au).

Funding: Np specific funding was required.

RESEARCH ARTICLE

Stylized facts of intraday precious metals

Jonathan Batten¹, Brian Lucey²*, Frank McGroarty³, Maurice Peat⁴, Andrew Urquhart⁵

1 Monash University Business School, Monash University, Caulfield, Victoria, Australia, 2 Trinity Business School, Trinity College Dublin, Dublin, Ireland, 3 Southampton Business School, University of Southampton, Southampton, United Kingdom, 4 University of Sydney Business School, Sydney, New South Wales, Australia, 5 Southampton Business School, University of Southampton, Southampton, United Kingdom

* blucey@tcd.ie

Abstract

This paper examines the stylized facts, correlation and interaction between volatility and returns at the 5-minute frequency for gold, silver, platinum and palladium from May 2000 to April 2015. We study the full sample period, as well as three subsamples to determine how high-frequency data of precious metals have developed over time. We find that over the full sample, the number of trades has increased substantially over time for each precious metal, while the bid-ask spread has narrowed over time, indicating an increase in liquidity and price efficiency. We also find strong evidence of periodicity in returns, volatility, volume and bid-ask spread. Returns and volume both experience strong intraday periodicity linked to the opening and closing of major markets around the world while the bid-ask spread is at its lowest when European markets are open. We also show a bilateral Granger causality between returns and volatility of each precious metal, which holds for the vast majority subsamples.

Introduction

This paper examines the intraday periodicity, correlation and volatility interaction in four precious metals markets. Our data set covers over 15-years of 5-minute data on gold, silver, platinum and palladium and finds significant evidence of intraday periodicity in returns, volatility, trading volumes and bid-ask spreads as well as strong evidence of bilateral Granger causality between returns and volatility. As well as being important in its own right in explaining highfrequency precious metal dynamics and trading behaviour, intraday periodicity, correlation and volatility interaction have important implications for investors trading precious metals intraday.

Gold is one of the most intensively traded assets, a feature not often understood by market participants. In 2011, estimated daily international turnover in gold was of the order of 4,000 metric tons, equivalent to a then average value of over \$240 billion. This is approximately the same as the daily dollar volume of trade on all of the world's stock exchanges combined [1]. If, as is common, we consider gold as a currency its turnover exceeds that in all but four currency pairs [2]. Gold trading is also highly concentrated, as it is in the foreign exchange market, with the two major centers for gold trading, London (physical, over-the-counter (LOTC) spot trade) and the New York Mercantile Exchange Futures Market (COMEX), totaling 85% (78.0% and 7.7% respectively) of global turnover value [3]. We study gold, silver, platinum and



Competing interests: The authors have declared that no competing interests exist.

palladium since they are the most traded due to them having ISO-4217 currency codes which means they are traded as a currency, see http://www.iso.org/iso/home/standards/currency_codes.htm

Our study is motivated by the fact that most financial time series exhibit periodicity. With high-frequency data the problem of periodicity becomes more complex since the entire form of the daily activity has to be taken into account. There is widespread empirical evidence that trading patterns vary systematically over the trading day and these patterns are highly correlated with intraday variations in returns, volatility, volume and bid-ask spreads in stock markets (for example see [4], [5], [6], [7], [8]), Foreign Exchange (FX) markets (see for example [9], [10], [11]) and Exchange Traded Funds (ETFs) (see for example [12]).

The finance literature has also shown that most intraday trading activity exhibits a Ushaped pattern, (for example [13] for Toronto stock exchange; [14] for the New York Stock Exchange (NYSE); [15] for the Tokyo stock exchange), while UK markets experience a Mshape where the volume is higher around the opening of US markets, see [16] and [17]. Also, [5] document a reverse J-shaped pattern of NYSE quotations and [18] support this pattern with London Stock Exchange (LSE) intraday spreads. Elevated opening and closing returns have been reflected in the volatility patterns, where a U-shape is found by [13], [19], [20] and [21].

This paper fills three lacunae in the literature. First, despite the extensive literature on periodicity in stock markets and FX markets, there is a notable lack of studies examining the periodicity of precious metals. [22] study the main stylized facts and dynamic properties of spot precious metals from 27th December 2008 to 30th November 2010 at 5-minute and 50-minute frequencies. They find clear evidence of periodic patterns matching the trading hours of the most active markets round-the-clock and therefore conclude that precious metals spot returns have similar properties to those of traditional financial assets. [23] examine the 5-minute gold futures market and find periodicity in absolute returns and the returns movements in response to macroeconomic announcements. [24] study the dynamic behaviour of six commodities, including gold, and find that intraday returns have long memory. [25] study high-frequency futures data for gold, silver and copper from 1999 to 2008 through four measures of volatility and find that each of the return distributions are not normal. [3] examine the gold markets and find intraday periodicity in the context of how the London and New York markets interrelate. Given the size of the market, there remains a lack of studies examining the intraday periodicity of precious metals spot rates, this study seeks to fill this gap.

Second, a further gap in the literature revolves around the well-known stylised fact in finance that stock index returns are negatively correlated with changes in volatility [26]. This distinctive cross dependence pattern plays an essential role in the development of volatility as an asset class, in modelling volatility and in option pricing. Many studies have examined this phenomenon in stock markets, see [27], [28], [29], [30], [31]. However, there are to our knowledge no extant studies that study this relationship in precious metals at a high-frequency.

A third gap relates to the evaluation of intraday features in over the counter trades. By contrast to futures markets, where there is a great deal of research across a large number of assets, over the counter markets have received much less attention. In the area of gold the only comparable study to this paper is that of [32]. A frequent assumption of over the counter market analysis is that the over the counter market is illiquid see [33] and [34]. That is not the case here.

Transparency in the OTC markets are typically rather low. There is no public record of trade volumes or prices, only the quotes are observable. For gold, this lack of transparency was the genesis of the Loco London Liquidity Survey [35] which has gone some way to

demonstrate gold as a liquid asset. Evidence in this paper on bid-ask spread and volume will therefore be of use to fill this gap.

This paper considers the intraday patterns in the returns, volatility, volume and the bid-ask spread of gold, silver, platinum and palladium at a 5-minute frequency from May 2000 to April 2015. The intraday patterns of precious metals have not received detailed empirical attention in the literature, which is all the more surprising given the growth of precious metals as investment assets as well as the growth of high-frequency trading. This paper also investigates the lead-lag relationship and Granger causality between returns and volatility of precious metals at high frequency, an area currently unexplored.

Therefore, this study contributes to the literature in a number of ways. Firstly, this is the first study to examine the stylized facts of all precious metals at high frequency over a long sample period. [22] study high-frequency precious metals from December 2008 to November 2010, which may not be the best time to determine the stylized facts of precious metals given the aftermath of the financial crisis. Secondly, by splitting our data into three equally-sized subsamples, we also study how the stylized facts of precious metals have developed over time in a dynamic framework. Thirdly, we document the intraday periodicity of precious metals which can offer valuable information to investors trading precious metals. Fourthly, we also study the relationship between returns and volatility of high-frequency precious metals, which has been unexplored in the empirical literature.

The remainder of the paper is organized in as follows. The next section presents the data and methodology while Section 3 reports the empirical results. Section 4 reports the empirical results while Section 5 summarises the findings and provides conclusions.

Material and methods

The data is collected from Thomson Reuters Tick History for the period 1st May 2000 to 30th April 2015 and consist of the closing prices, time stamp, the bid/ask price, and the number of trades for gold, silver, platinum and palladium. These prices are made by wholesale market practitioners with prices and trades time-stamped as they arise in online trading platforms.

In order to examine the periodicity of these precious metals, it is important to use short enough intervals to capture the high frequency behaviour of the data, but at the same time long enough to avoid any undue noise [36]. Therefore, we follow [37] who suggests that 5-minute intervals are the best compromise. The markets of all four precious metals trade from Sunday 22.00 to Friday with a daily break between 21.00 and 22.00 GMT. We filter the data by removing any errors caused by missing bid/ask data and also remove any data when the market is closed.

Given our large sample period, the increased attention to precious as an investment and attention in the academic literature, the stylized facts may change over our 15-year full sample period. Therefore as well as studying the full sample period, we also split our sample into three equal-sized subsamples, from 1st May 2000 to 30th April 2005, 1st May 2005 to 30th April 2010 and 1st May 2010 to 30th April 2015.

The variables of interest in this paper are returns, volume, volatility and the bid-ask spread (BAS). From 5-minute transaction prices of each precious metal, we calculate the return following [38] such that;

$$\mathbf{r}_{t,d} = (\ln \ CP_{t,d} - \ln \ CP_{t,d-1}) \times 100 \tag{1}$$

where $r_{t,d}$ is the return for the intraday period *d* on trading day *t* and $CP_{t,d}$ is the closing price for the intraday period *d* on trading day *t*. Following [5] and [39], we calculate the bid-ask

spread as the difference in prices;

$$BAS_i = \frac{ASK_i - BID_i}{(ASK_i + BID_i)/2}$$
(2)

where ASK_i is the ask price of precious metal *i* and BID_i is the bid price of precious metal *i*. Given that true volatility is unobservable, the empirical results may be sensitive to the chosen volatility measure. In this paper, the intraday volatility is calculated using three approaches;

$$VO_t^{SQ} = ln \left(\frac{CP_t}{CP_{t-1}}\right)^2 \tag{3}$$

$$VO_t^{GK} = 0.5 \left[ln(HP_t) - ln(LP_t) \right]^2 - \left[2ln2 - 1 \right] \left[ln(CP_t) - ln(OP_t) \right]^2$$
(4)

$$VO_t^{RS} = [ln(HP_t - ln(OP_t))][ln(HP_t) - ln(CP_t)] + [ln(LP_t) - ln(OP_t)][ln(LP_t) - ln(CP_t)]$$
(5)

Where VO_t^{SQ} , VO_t^{GK} and VO_t^{RS} are the square return, volatility proposed by [40], and the volatility of [41] and [42]. *HP*, *LP*, *CP* and *OP* represent the high price, low price, closing price and opening price respectively. These different measures of volatility are calculated in different ways and therefore may provide differing results. The GK and RS measures that take into account the high, low, opening and closing prices of the precious metals when calculating volatility while the SQ measure just takes into account the returns of the precious metals. The GK and RS measures guard against the potential distorting impact of high-frequency real-world frictions by incorporating range information in the estimation of volatility, while the SQ measure does not. Therefore, although all three measures do calculate volatility, they do so in a slightly different manner and consequently may provide contrasting results.

The time-series graph of each of the precious metals prices is reported in Fig 1, where the four precious metals seem to follow a similar pattern over time. We can see that silver has been very volatile and that palladium's value is much less than the other three precious metals. Gold and silver have followed very similar paths since 2012 and that all four were affected by the 2008 global financial crisis. Fig 2 presents the volume of trades of each precious metal over time and we can see that each precious metal experiences a large increase in the number of trades throughout the sample period. It is also evident that gold has the largest volume of





https://doi.org/10.1371/journal.pone.0174232.g001



trades, followed by silver, platinum and palladium, which is also reported in Tables 1 and 2. The BAS are reported in Fig 3 and all precious show a large BAS at the beginning of the sample period. The spread does decreases after May 2003 for all precious metals and stays low throughout the sample period, except a sharp increase in the spread during the 2008 global financial crisis. Fig 4 reports the squared returns measure for volatility and shows that volatility for each precious metal was highest during the 2008 global financial crisis and at certain points in the early 2000s. Volatility is relatively low from 2010 to 2015, which may be due to the increase in volume of trading and thus efficiency.

Results

This section provides the results for the stylized facts of gold, silver, platinum and palladium returns, volatility, volume and BAS.

Full sample descriptive statistics

The descriptive statistics for the return series, the volatility measures, volume and BAS for the full sample period of the four precious metals are reported in <u>Table 1</u>. Panel A shows gold is the only precious metal to report a positive mean return over are sample period while platinum has the highest negative mean return and palladium the least negative mean return. Gold returns are also the least volatile of the precious metals while palladium is found to be the most volatile. This is consistent with the finding of [22] that gold has a larger interest than other precious metals that may lead to higher efficiency compared to other precious metals, which leads to smaller risk. The kurtosis of gold is much higher than other precious metals with silver having the lowest kurtosis. All precious metals have negative skewness, which is behaviour similar to that observed in equities.



Table 1. Descriptive statistics for the full sample gold, silver, platinum and palladium. 'SQ' denotes the squared returns measure of volatility, 'GK' denotes the Garman-Klass measure while 'RS' denotes the Rogers-Satchell measure.

Panel A: Returns Mean 0.000901 -0.0000231 -0.0000507 -0.0001706 Std 0.0796037 0.162851 0.2070907 0.4134391 Kurt 85.36 67.57 212.65 44.37 Skew -0.6 -1.14 -1.25 -0.99 5% quant 0.0306469 -0.244998 -0.271639 -0.4814728 25% quant 0.1053416 -0.0516929 0 0 50% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{GQ} U U 0 0 0 Mean 0.000006 0.0265204 0.0428665 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 7953.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0		XAU	XAG	ХРТ	XPD
Mean 0.0000901 -0.0000231 -0.0000507 -0.0001706 Std 0.0796037 0.162851 0.2070907 0.4134391 Kurt 85.36 67.57 212.65 44.37 Skew -0.6 -1.14 -1.25 -0.99 5% quant 0.0306469 -0.244998 -0.271639 -0.4814728 25% quant 0.1053416 -0.0516929 0 0 50% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{6O} 0 0 0 0 Mean 0.000006 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 5% quant 0	Panel A: Returns				
Std 0.0796037 0.162851 0.2070907 0.4134391 Kurt 85.36 67.57 212.65 44.37 Skew -0.6 -1.14 -1.25 -0.99 5% quant 0.0306469 -0.244998 -0.271639 -0.4814728 25% quant 0.1053416 -0.0516929 0 0 50% quant 0 0 0 0 75% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ⁶⁰ 0 0 0 0 0 Mean 0.000006 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 <td>Mean</td> <td>0.0000901</td> <td>-0.0000231</td> <td>-0.0000507</td> <td>-0.0001706</td>	Mean	0.0000901	-0.0000231	-0.0000507	-0.0001706
Kurt 85.36 67.57 212.65 44.37 Skew -0.6 -1.14 -1.25 -0.99 5% quant 0.0306469 -0.244998 -0.271639 -0.4814728 25% quant 0.1053416 -0.0516929 0 0 50% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{SO} 0.000006 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000005 0.0227153 0.0174024 0.9005	Std	0.0796037	0.162851	0.2070907	0.4134391
Skew -0.6 -1.14 -1.25 -0.99 5% quant 0.0306469 -0.244998 -0.271639 -0.4814728 25% quant 0.1053416 -0.0516929 0 0 50% quant 0 0 0 0 50% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{SQ} 0 0.0428865 0.1709317 Mean 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 50% quant 0.000005 0.0227153 0.0143255 0.017405 95% quant 0.000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1	Kurt	85.36	67.57	212.65	44.37
5% quant 0.0306469 -0.244998 -0.271639 -0.4814728 25% quant 0.1053416 -0.0516929 0 0 50% quant 0 0 0 0 0 50% quant 0.1053416 -0.0516929 0 0 0 75% quant 0.0306469 0.0579207 0.0059419 0 0 95% quant 0.1053416 0.220995 0.2757941 0.558661 Panel B: Vol ^{SQ} 0.0000066 0.0265204 0.0428865 0.1709317 Mean 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 50% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000005 0.0227153 0.012782 </td <td>Skew</td> <td>-0.6</td> <td>-1.14</td> <td>-1.25</td> <td>-0.99</td>	Skew	-0.6	-1.14	-1.25	-0.99
25% quant 0.1053416 -0.0516929 0 0 50% quant 0 0 0 0 0 75% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{SQ} 0.000006 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 0 25% quant 0.0000001 0.0030575 0 0 0 5% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} 0.0152828 0.0127282 0.0142494 Std 0.0265717 0.037425 <td>5% quant</td> <td>0.0306469</td> <td>-0.244998</td> <td>-0.271639</td> <td>-0.4814728</td>	5% quant	0.0306469	-0.244998	-0.271639	-0.4814728
50% quant 0 0 0 0 75% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{SQ} 0.000006 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 129184.22 Kurt 82650.17 89129.77 79533.57 129184.22 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 5% quant 0.000001 0.0030575 0 0 75% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} 0.0152828 0.0127282 0.0142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7<	25% quant	0.1053416	-0.0516929	0	0
75% quant 0.0306469 0.0579207 0.0059419 0 95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{SQ} 0.0000066 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 25% quant 0 0 0 0 5% quant 0.0000001 0.0030575 0 0 5% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.00000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} 0.0142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192	50% quant	0	0	0	0
95% quant 0.1053416 0.229095 0.2757941 0.558661 Panel B: Vol ^{SQ} Mean 0.000006 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 50% quant 0.000001 0.0030575 0 0 75% quant 0.0000023 0.01227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} Vol ^{GK} Vol Vol Vol Mean 0.0075703 0.0152828 0.0127282 0.0142494 Mean 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3	75% quant	0.0306469	0.0579207	0.0059419	0
Panel B: Vol ^{SQ} Mean 0.000006 0.0265204 0.0428865 0.1709317 Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 5% quant 0.000001 0.0030575 0 0 75% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} U U U U U Mean 0.0075703 0.0152828 0.0127282 0.0142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3	95% quant	0.1053416	0.229095	0.2757941	0.558661
Mean 0.000006 0.0265204 0.0428865 0.1709317 Std 0.000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 5% quant 0.0000001 0.0030575 0 0 5% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} Vol ^{GK} Vol 0.0142494 0.00142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Panel B: Vol ^{SQ}	- ·	·		·
Std 0.0000059 0.2211995 0.6283358 1.1639475 Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 5% quant 0.0000001 0.0030575 0 0 5% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} 2 0.0152828 0.0127282 0.0142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Mean	0.000006	0.0265204	0.0428865	0.1709317
Kurt 82650.17 89129.77 79533.57 129184.22 Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 25% quant 0 0 0 0 5% quant 0 0 0 0 5% quant 0.0000001 0.0030575 0 0 5% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} 2 2 0.0142494 0.9005991 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Std	0.0000059	0.2211995	0.6283358	1.1639475
Skew 227.69 240.32 249.7 258.3 5% quant 0 0 0 0 0 25% quant 0 0 0 0 0 0 25% quant 0 0 0 0 0 0 0 50% quant 0.0000001 0.0030575 0 0 0 0 75% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} 0.0075703 0.0152828 0.0127282 0.0142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Kurt	82650.17	89129.77	79533.57	129184.22
5% quant 0 0 0 0 25% quant 0 0 0 0 0 0 50% quant 0.0000001 0.0030575 0 0 0 75% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 9sequent 0.0075703 0.0152828 0.0127282 0.0142494 Mean 0.00265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Skew	227.69	240.32	249.7	258.3
25% quant 0 0 0 0 50% quant 0.0000001 0.0030575 0 0 75% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK}	5% quant	0	0	0	0
50% quant 0.0000001 0.0030575 0 0 75% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK}	25% quant	0	0	0	0
75% quant 0.0000005 0.0227153 0.0143255 0.017405 95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK}	50% quant	0.0000001	0.0030575	0	0
95% quant 0.0000023 0.1054145 0.1758024 0.9005991 Panel C: Vol ^{GK} <td< td=""><td>75% quant</td><td>0.0000005</td><td>0.0227153</td><td>0.0143255</td><td>0.017405</td></td<>	75% quant	0.0000005	0.0227153	0.0143255	0.017405
Mean 0.0075703 0.0152828 0.0127282 0.0142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	95% quant	0.000023	0.1054145	0.1758024	0.9005991
Mean 0.0075703 0.0152828 0.0127282 0.0142494 Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Panel C: Vol ^{GK}				
Std 0.0265717 0.037425 0.0164499 0.0213277 Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Mean	0.0075703	0.0152828	0.0127282	0.0142494
Kurt 88192.25 36409.7 115.87 42.3 Skew 283.82 173.29 4.74 3.81	Std	0.0265717	0.037425	0.0164499	0.0213277
Skew 283.82 173.29 4.74 3.81	Kurt	88192.25	36409.7	115.87	42.3
	Skew	283.82	173.29	4.74	3.81
o% yuanı U U U U	5% quant	0	0	0	0
25% quant 0.0026343 0.0028133 0 0	25% quant	0.0026343	0.0028133	0	0
50% quant 0.0063165 0.0124145 0.0063408 0.0040314	50% quant	0.0063165	0.0124145	0.0063408	0.0040314
75% quant 0.010535 0.0233759 0.0223845 0.0242976	75% quant	0.010535	0.0233759	0.0223845	0.0242976
95% quant 0.0192804 0.0409709 0.0415909 0.051246	95% quant	0.0192804	0.0409709	0.0415909	0.051246
Panel D: Vol ^{RS}	Panel D: Vol ^{RS}				
Mean 0.007523 0.0150185 0.0125224 0.0125509	Mean	0.007523	0.0150185	0.0125224	0.0125509
Std 0.0370348 0.0159083 0.0169529 0.0212931	Std	0.0370348	0.0159083	0.0169529	0.0212931
Kurt 93433.62 74.61 17.39 52.94	Kurt	93433.62	74.61	17.39	52.94
Skew 296.35 2.84 2.1 3.52	Skew	296.35	2.84	2.1	3.52
5% quant 0 0 0 0	5% quant	0	0	0	0
25% quant 0.001585 0 0 0	25% quant	0.001585	0	0	0
50% quant 0.0063565 0.0125744 0 0	50% quant	0.0063565	0.0125744	0	0
75% quant 0.0107109 0.0245575 0.0237169 0.0210129	75% quant	0.0107109	0.0245575	0.0237169	0.0210129
95% quant 0.0197609 0.042643 0.0442581 0.0533983	95% quant	0.0197609	0.042643	0.0442581	0.0533983
Panel E: Volume	Panel E: Volume				
Mean 21.9704 13.2289 6.1089 3.7997	Mean	21.9704	13.2289	6.1089	3.7997
Std 27.2509 22.2185 11.6664 106.15	Std	27.2509	22.2185	11.6664	106.15
Kurt 3.36 2082.75 4842.18 121075.1	Kurt	3.36	2082.75	4842.18	121075.1
Skew 1.64 12.47 20.91 346.2	Skew	1.64	12.47	20.91	346.2
5% quant 0 0 0 0	5% quant	0	0	0	0

(Continued)



Table 1. (Continued)

	XAU	XAG	ХРТ	XPD
25% quant	1	0	0	0
50% quant	10	3	0	0
75% quant	37	19	9	4
95% quant	75	52	27	17
Panel F: BAS				
Mean	0.0012838	0.0038627	0.0068356	0.0173066
Std	0.000765	0.0176961	0.010543	0.0109459
Kurt	162.94	12592.23	30361.7	3988.74
Skew	4.97	111.66	-146.85	22.96
5% quant	0.000438	0.0012642	0.0029789	0.0066687
25% quant	0.0006769	0.0025233	0.004324	0.0084034
50% quant	0.0012001	0.0037922	0.0057904	0.0148368
75% quant	0.0017833	0.0044623	0.0081533	0.0234192
95% quant	0.0023684	0.0069136	0.0149254	0.0377358
Obs	1,079,830	1,079,750	1,079,679	1,079,688

https://doi.org/10.1371/journal.pone.0174232.t001

Panels B, C and D of Table 1 report the descriptive statistics for the volatility measures of the four precious metals. The SQ measure suggests that platinum has the highest mean volatility, while the GK and RS measures both suggest that silver has the highest mean volatility. Gold has the highest positive kurtosis according to the GK and RS measures, while the SQ measure suggests that palladium has the highest kurtosis. All four precious metals volatility measures have positive skewness, with the SQ measure attributing the highest skewness to palladium, while the GK and RS measures suggest that gold has the highest skewness. Panel E of Table 1 reports the descriptive statistics of the volume of trades and shows that gold has the largest mean volume and palladium has the highest variation in volume, followed by silver, platinum and palladium. All four precious metals volume measures have excess kurtosis and positive skewness, which increases as the number of trades fall. The BAS analysis of the precious metals is reported in Panel F of Table 1 and shows that platinum has the largest mean spread, followed by silver, palladium and finally gold. Gold has the smallest mean standard deviation of BAS while silver has the greatest. The kurtosis of each precious metals BAS indicates leptokurtic distributions and positive skewness.

Overall, from the full sample analysis we can see that gold has the highest mean return and seems the most liquid since it has the highest mean volume and lowest mean BAS over the full sample. Palladium seems the least liquid precious metal with the lowest mean volume and highest mean BAS.

Subsample descriptive statistics

In order to see how the stylized facts of these precious metals have behaved over our sample period, we split the full sample period into three equal sub-periods and repeat the analysis reported in Table 1. The results are reported in Table 2 for gold and silver and Table 3 for platinum and palladium.

Table 2 reports the sub-sample analysis of the descriptive statistics of gold and shows that the 2005–2010 period had the largest mean return, while the 2010–2015 period had a negative mean return. The 2005–2010 period also had the largest standard deviation, the highest kurtosis and largest negative skewness of the three sub-samples. In the 2010–2015 period for gold,



Table 2. Descriptive statistics for gold and silver over the three subsamples. 'SQ' denotes the squared returns measure of volatility, 'GK' denotes the Garman-Klass measure while 'RS' denotes the Rogers-Satchell measure.

2000-2005 2005-2010 2010-2015 2000-2005 2005-2010 2010-2015 Panel A: Returns		XAU			XAG			
Panel A: Returns Mean 0.0001539 0.0001586 -0.0000423 0.0001313 -0.000046 -0.0001547 Std 0.0781752 0.0911624 0.0677261 0.1545071 0.1856633 0.1456374 Kurt 43.64 106.39 60.87 81.44 36.9 115.62 Skew -0.52 -0.94 0.16 -0.98 -1.2 -1.14 5% quant -0.0139772 -0.0329164 -0.0260909 0 -0.027361 25% quant 0.0621311 50% quant 0.0619195 98% quant 0.0028111 0.0366622 0.0264651 0 0.0344708 0.0212102 Std 0.0265623 52354.51 27800.73 48209.64		2000–2005	2005–2010	2010-2015	2000–2005	2005–2010	2010-2015	
Mean 0.0001539 0.0001586 -0.0000423 0.0001313 -0.00046 -0.0001547 Std 0.0781752 0.0911824 0.0677261 0.1545071 0.1856633 0.1456374 Kurt 43.64 106.39 60.87 81.44 36.9 115.62 Skew -0.52 -0.94 0.16 -0.98 -1.2 -1.14 5% quant -0.0139772 -0.0329164 -0.0260909 0 -0.0743218 -0.0621311 50% quant 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0.026131 0.02619195 95% quant 0.100007 0.123224 0.026651 0 0.073332 0.208877 Panel B: Vol ^{SO} -0.026161 0 0.073332 0.208877 0.0343724 0.0244708 0.0212102 Std 0.0412832 0.0665177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt<	Panel A: Returns							
Std 0.0781752 0.0911624 0.0677261 0.1545071 0.1856633 0.1456374 Kurt 43.64 106.39 60.87 81.44 36.9 115.62 Skew -0.52 -0.94 0.16 -0.98 -1.2 -1.14 5% quant -0.013098 -0.1290822 -0.0926088 -0.239318 -0.291971 -0.207361 25% quant -0.0139772 -0.0326144 -0.0260909 0 -0.0743218 -0.0621311 50% quant 0.0280181 0.0369622 0.0264651 0 0.0783392 0.061195 95% quant 0.100007 0.123224 0.0927663 0.223464 0.277393 0.208877 Panel B: Vol ^{SO} - - - 0.0363964 0.0241708 0.0212102 Std 0.0412832 0.0865177 0.0363964 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31	Mean	0.0001539	0.0001586	-0.0000423	0.0001313	-0.000046	-0.0001547	
Kurt43.64106.3960.8781.4436.9115.62Skew-0.52-0.940.16-0.98-1.2-1.145% quant-0.131098-0.1290822-0.0926088-0.233918-0.291971-0.20736125% quant-0.0139772-0.0329164-0.02609090-0.0743218-0.062131150% quant000000075% quant0.026019150.026465100.07833920.061919595% quant0.1000070.12322240.09276630.2234640.2773930.208877Panel B: Vol ^{SO}	Std	0.0781752	0.0911624	0.0677261	0.1545071	0.1856633	0.1456374	
Skew -0.52 -0.94 0.16 -0.98 -1.2 -1.14 5% quant -0.131098 -0.1290822 -0.0926088 -0.233918 -0.291971 -0.207361 25% quant -0.0139772 -0.0329164 -0.0260909 0 -0.0743218 -0.0621311 50% quant 0 0 0 0 0 0 0 75% quant 0.02280181 0.0369622 0.0264651 0 0.0783392 0.0619195 95% quant 0.100007 0.1232224 0.0927663 0.223464 0.277393 0.208877 Panel B: Vol ^{SQ} -0.0412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2200389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew119.76196.31129.54 185.24 174.42 340.88 5% quant 0 0 0 0 0 0 25% quant 0 0.0001551 0.0001233 0 0 0.0009529 50% quant 0.0062739 0.005627 0.002779 0.025591 0.0288249 0.0164745 95% quant 0.0062739 0.005627 0.002779 0.025551 0.0288249 0.0164745 95% quant 0.006627 0.002779 0.025551 0.0288249 0.0164745 95% quant 0.006634 0.0491831 0.01417717 0.0238685 Std 0.005634 0.049173 0.0095536 0.0720	Kurt	43.64	106.39	60.87	81.44	36.9	115.62	
5% quant -0.131098 -0.1290822 -0.0926088 -0.233918 -0.291971 -0.207361 25% quant -0.0139772 -0.0329164 -0.0260909 0 -0.0743218 -0.0621311 50% quant 0 0 0 0 0 0 0 75% quant 0.0280181 0.0369622 0.0264651 0 0.0783392 0.0619195 95% quant 0.100007 0.123224 0.0927663 0.223464 0.277393 0.208877 Panel B: Vol ⁶⁰ 0.0061114 0.0083106 0.0045868 0.0238724 0.0344708 0.0212102 Std 0.0412832 0.0865177 0.0363694 0.2180535 0.215014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0 0 0 0 0.0002529 50% (qu	Skew	-0.52	-0.94	0.16	-0.98	-1.2	-1.14	
25% quant -0.0139772 -0.0329164 -0.0260909 0 -0.0743218 -0.0621311 50% quant 0 0 0 0 0 0 0 0 75% quant 0.0260181 0.0369622 0.0264651 0 0.0783392 0.0619195 95% quant 0.100007 0.1232224 0.0927663 0.223464 0.277393 0.208877 Panel B: Vol ^{SO} 0.0344708 0.021102 Std 0.0412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0 0 0 0 0 25% quant 0 0 0.0000513 0.0001531 0.000251 0.0025591 0.0288249 0.0164745 95% quant 0.002627 0.0027779	5% quant	-0.131098	-0.1290822	-0.0926088	-0.233918	-0.291971	-0.207361	
50% quant 0 0 0 0 0 0 75% quant 0.0280181 0.0369622 0.0264651 0 0.0783392 0.0619195 95% quant 0.100007 0.1232224 0.0927663 0.223464 0.277393 0.208877 Panel B: Vol ^{SO} 0.0061114 0.0083106 0.0045868 0.0238724 0.0344708 0.0212102 Std 0.0412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0 0 0 0 0.0009529 50% quant 0.0005131 0.001515 0.0002779 0.0255591 0.0288249 0.0164745 95% quant 0.0026273 0.002779 0.0255591 0.0288249 0.0164745 95% quant 0.00230615	25% quant	-0.0139772	-0.0329164	-0.0260909	0	-0.0743218	-0.0621311	
75% quant 0.0280181 0.0369622 0.0264651 0 0.0783392 0.0619195 95% quant 0.100007 0.1232224 0.0927663 0.223464 0.277393 0.208877 Panel B: Vol ^{SQ} 0.0045868 0.0238724 0.0344708 0.0212102 Std 0.00412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 118.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0.000004 0 0 0 25% quant 0 0.0001551 0.0001293 0 0 0.00038483 75% quant 0.0026279 0.005627 0.0027779 0.0255591 0.0288249 0.0164745 95% quant 0.0023015 0.0308749 0.0166092 0.095536 0.1418637 0.07761584 Panel C: Vol ^{GK}	50% quant	0	0	0	0	0	0	
95% quant 0.100007 0.1232224 0.0927663 0.223464 0.277393 0.208877 Panel B: Vol ^{SQ} 0.0061114 0.0083106 0.0045868 0.0238724 0.0344708 0.0212102 Std 0.0412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0.0000004 0 0 0 25% quant 0 0.0012179 0.0006903 0 0.0058316 0.0038483 75% quant 0.00230615 0.0308749 0.0166092 0.0955546 0.147454 95% quant 0.00230615 0.0308749 0.0166092 0.0955546 0.147717 0.0238685 Std 0.0042371 0.0089173 0.0095908 0.0491881 0.0147717 0.02386	75% quant	0.0280181	0.0369622	0.0264651	0	0.0783392	0.0619195	
Panel B: Vol ^{SQ} Mean 0.0061114 0.0083106 0.0045868 0.0238724 0.0344708 0.0212102 Std 0.0412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0.0000004 0 0 0 25% quant 0 0.0001517 0.0006903 0 0.0058316 0.0038483 5% quant 0.0062739 0.005627 0.002779 0.0255591 0.0288249 0.0164745 95% quant 0.0230615 0.0308749 0.0166092 0.0955546 0.1418637 0.0761584 Panel C: Vol ^{GK} Vol ^{GK} Vol ^{GK} Vol 0.0044597 0.0095908 0.0491881 0.014174 0.038006 Kurt 11.53 33674.9 16676.48 26452.65 9.36 28674.04<	95% quant	0.100007	0.1232224	0.0927663	0.223464	0.277393	0.208877	
Mean 0.0061114 0.0083106 0.0045868 0.0238724 0.0344708 0.0212102 Std 0.0412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0.0000004 0 0 0 25% quant 0 0.0001551 0.0001293 0 0 0.0009529 50% quant 0.0005131 0.0012179 0.00255591 0.0288249 0.0164745 95% quant 0.0230615 0.0308749 0.0166092 0.095536 0.1418637 0.0761584 Panel C: Vol ^{GK} Vol ^{GK} Vol ^{GK} Vol ^{GK} Vol ^{GK} 0.0442371 0.0089173 0.0095536 0.0072037 0.0147717 0.0238685 Std 0.0056034 0.0444597 0.0095908 0.0491881 0.014154 0.038006	Panel B: Vol ^{SQ}		·					
Std 0.0412832 0.0865177 0.0363694 0.2180535 0.2150014 0.2300389 Kurt 22665.23 52354.51 27800.73 48209.64 46520.06 154210.01 Skew 119.76 196.31 129.54 185.24 174.42 340.88 5% quant 0 0 0.0000004 0 0 0 25% quant 0 0.0001551 0.0001293 0 0 0.0009529 50% quant 0.0005131 0.0012179 0.0006903 0 0.00288249 0.0164745 95% quant 0.0230615 0.0308749 0.0166092 0.0955546 0.1418637 0.0761584 Panel C: Vol ^{GK} 0.0444597 0.0095536 0.0072037 0.0147717 0.0238685 Std 0.0056034 0.0444597 0.0095908 0.0491881 0.014154 0.038006 Kurt 11.53 33674.9 16676.48 26452.65 9.36 28674.04 Skew 2.39 <td>Mean</td> <td>0.0061114</td> <td>0.0083106</td> <td>0.0045868</td> <td>0.0238724</td> <td>0.0344708</td> <td>0.0212102</td>	Mean	0.0061114	0.0083106	0.0045868	0.0238724	0.0344708	0.0212102	
Kurt22665.2352354.5127800.7348209.6446520.06154210.01Skew119.76196.31129.54185.24174.42340.885% quant000.000000400025% quant00.00015510.0001293000.000952950% quant0.00051310.00121790.000690300.00583160.003848375% quant0.00627390.0056270.00277790.02555910.02882490.016474595% quant0.02306150.03087490.01660920.09555460.14186370.0761584Panel C: Vol ^{GK} </td <td>Std</td> <td>0.0412832</td> <td>0.0865177</td> <td>0.0363694</td> <td>0.2180535</td> <td>0.2150014</td> <td>0.2300389</td>	Std	0.0412832	0.0865177	0.0363694	0.2180535	0.2150014	0.2300389	
Skew119.76196.31129.54185.24174.42340.88 5% quant000.0000004000 25% quant00.00015510.0001293000.0009529 50% quant0.00051310.00121790.000690300.00583160.0038483 75% quant0.00627390.0056270.00277790.02555910.02882490.0164745 95% quant0.02306150.03087490.01660920.09555460.14186370.0761584Panel C: Vol ^{GK} Mean0.00423710.00891730.00955360.00720370.01477170.0238685Std0.00560340.04445970.00959080.04918810.0141540.038006Kurt11.5333674.916676.4826452.659.3628674.04Skew2.39180.48106.98155.42.18160.03 5% quant000.00334378000.0066652025% quant00.00356230.005989500.001141790.022427275% quant0.0021060.0067490.008516700.01144790.022427275% quant0.00634650.01162340.01172610.01064430.02064880.03030595% quant0.01531370.02284460.01901010.02941070.04062440.0450477	Kurt	22665.23	52354.51	27800.73	48209.64	46520.06	154210.01	
5% quant 0 0 0.0000004 0 0 0 25% quant 0 0.0001551 0.0001293 0 0 0.0009529 50% quant 0.0005131 0.0012179 0.0006903 0 0.0058316 0.0038483 75% quant 0.0062739 0.005627 0.0027779 0.0255591 0.0288249 0.0164745 95% quant 0.0230615 0.0308749 0.0166092 0.0955546 0.1418637 0.0761584 Panel C: Vol ^{GK} 0.0147717 0.0238685 Std 0.0042371 0.0089173 0.0095536 0.0072037 0.0147717 0.0238685 Std 0.0056034 0.0444597 0.0095908 0.0491881 0.014154 0.038006 Kurt 11.53 33674.9 16676.48 26452.65 9.36 28674.04 Skew 2.39 180.48 106.98 155.4 2.18 160.03 5% quant 0 0 0.0035623 0.0059895	Skew	119.76	196.31	129.54	185.24	174.42	340.88	
25% quant00.00015510.0001293000.000952950% quant0.00051310.00121790.000690300.00583160.003848375% quant0.00627390.0056270.00277790.02555910.02882490.016474595% quant0.02306150.03087490.01660920.09555460.14186370.0761584Panel C: Vol ^{GK} </td <td>5% quant</td> <td>0</td> <td>0</td> <td>0.000004</td> <td>0</td> <td>0</td> <td>0</td>	5% quant	0	0	0.000004	0	0	0	
50% quant0.00051310.00121790.000690300.00583160.003848375% quant0.00627390.0056270.00277790.02555910.02882490.016474595% quant0.02306150.03087490.01660920.09555460.14186370.0761584Panel C: Vol ^{GK} Mean0.00423710.00891730.00955360.00720370.01477170.0238685Std0.00560340.04445970.00959080.04918810.0141540.038006Kurt11.5333674.916676.4826452.659.3628674.04Skew2.39180.48106.98155.42.18160.035% quant000.0034378000.0066652025% quant00.0067490.008516700.01144790.022427275% quant0.00634650.01162340.01172610.01064430.02064880.030330595% quant0.01531370.02284460.01901010.02941070.04062440.0450477	25% quant	0	0.0001551	0.0001293	0	0	0.0009529	
75% quant0.00627390.0056270.00277790.02555910.02882490.016474595% quant0.02306150.03087490.01660920.09555460.14186370.0761584Panel C: Vol ^{GK} Mean0.00423710.00891730.00955360.00720370.01477170.0238685Std0.00560340.04445970.00959080.04918810.0141540.038006Kurt11.5333674.916676.4826452.659.3628674.04Skew2.39180.48106.98155.42.18160.035% quant000.0034378000.0066652025% quant00.0067490.008516700.001144790.022427275% quant0.00634650.01162340.01172610.01064430.02064880.030330595% quant0.01531370.02284460.01901010.02941070.04062440.0450477	50% quant	0.0005131	0.0012179	0.0006903	0	0.0058316	0.0038483	
95% quant 0.0230615 0.0308749 0.0166092 0.0955546 0.1418637 0.0761584 Panel C: Vol ^{GK}	75% quant	0.0062739	0.005627	0.0027779	0.0255591	0.0288249	0.0164745	
Panel C: Vol ^{GK} Mean 0.0042371 0.0089173 0.0095536 0.0072037 0.0147717 0.0238685 Std 0.0056034 0.0444597 0.0095908 0.0491881 0.014154 0.038006 Kurt 11.53 33674.9 16676.48 26452.65 9.36 28674.04 Skew 2.39 180.48 106.98 155.4 2.18 160.03 5% quant 0 0 0.0035623 0.0059895 0 0.0048847 0.0151101 50% quant 0.002106 0.006749 0.0085167 0 0.0114479 0.0224272 75% quant 0.0063465 0.0116234 0.0117261 0.0106443 0.0206488 0.0303305 95% quant 0.0153137 0.0228446 0.0190101 0.0294107 0.0406244 0.0450477	95% quant	0.0230615	0.0308749	0.0166092	0.0955546	0.1418637	0.0761584	
Mean0.00423710.00891730.00955360.00720370.01477170.0238685Std0.00560340.04445970.00959080.04918810.0141540.038006Kurt11.5333674.916676.4826452.659.3628674.04Skew2.39180.48106.98155.42.18160.035% quant000.0034378000.0066652025% quant00.00356230.005989500.001144790.015110150% quant0.0021060.0067490.008516700.01144790.022427275% quant0.00634650.01162340.01172610.01064430.02064880.030330595% quant0.01531370.02284460.01901010.02941070.04062440.0450477	Panel C: Vol ^{GK}							
Std0.00560340.04445970.00959080.04918810.0141540.038006Kurt11.5333674.916676.4826452.659.3628674.04Skew2.39180.48106.98155.42.18160.035% quant000.0034378000.0066652025% quant00.00356230.005989500.00488470.015110150% quant0.0021060.0067490.008516700.01144790.022427275% quant0.00634650.01162340.01172610.01064430.02064880.030330595% quant0.01531370.02284460.01901010.02941070.04062440.0450477	Mean	0.0042371	0.0089173	0.0095536	0.0072037	0.0147717	0.0238685	
Kurt11.5333674.916676.4826452.659.3628674.04Skew2.39180.48106.98155.42.18160.035% quant000.0034378000.0066652025% quant00.00356230.005989500.00488470.015110150% quant0.0021060.0067490.008516700.01144790.022427275% quant0.00634650.01162340.01172610.01064430.02064880.030330595% quant0.01531370.02284460.01901010.02941070.04062440.0450477	Std	0.0056034	0.0444597	0.0095908	0.0491881	0.014154	0.038006	
Skew 2.39 180.48 106.98 155.4 2.18 160.03 5% quant 0 0 0.0034378 0 0 0.0066652 025% quant 0 0.0035623 0.0059895 0 0.0048847 0.0151101 50% quant 0.002106 0.006749 0.0085167 0 0.0114479 0.0224272 75% quant 0.0063465 0.0116234 0.0117261 0.0106443 0.0206488 0.0303305 95% quant 0.0153137 0.0228446 0.0190101 0.0294107 0.0406244 0.0450477	Kurt	11.53	33674.9	16676.48	26452.65	9.36	28674.04	
5% quant 0 0 0.0034378 0 0 0.0066652 025% quant 0 0.0035623 0.0059895 0 0.0048847 0.0151101 50% quant 0.002106 0.006749 0.0085167 0 0.0114479 0.0224272 75% quant 0.0063465 0.0116234 0.0117261 0.0106443 0.0206488 0.0303305 95% quant 0.0153137 0.0228446 0.0190101 0.0294107 0.0406244 0.0450477	Skew	2.39	180.48	106.98	155.4	2.18	160.03	
025% quant 0 0.0035623 0.0059895 0 0.0048847 0.0151101 50% quant 0.002106 0.006749 0.0085167 0 0.0114479 0.0224272 75% quant 0.0063465 0.0116234 0.0117261 0.0106443 0.0206488 0.0303305 95% quant 0.0153137 0.0228446 0.0190101 0.0294107 0.0406244 0.0450477	5% quant	0	0	0.0034378	0	0	0.0066652	
50% quant 0.002106 0.006749 0.0085167 0 0.0114479 0.0224272 75% quant 0.0063465 0.0116234 0.0117261 0.0106443 0.0206488 0.0303305 95% quant 0.0153137 0.0228446 0.0190101 0.0294107 0.0406244 0.0450477	025% quant	0	0.0035623	0.0059895	0	0.0048847	0.0151101	
75% quant 0.0063465 0.0116234 0.0117261 0.0106443 0.0206488 0.0303305 95% quant 0.0153137 0.0228446 0.0190101 0.0294107 0.0406244 0.0450477	50% quant	0.002106	0.006749	0.0085167	0	0.0114479	0.0224272	
95% quant 0.0153137 0.0228446 0.0190101 0.0294107 0.0406244 0.0450477	75% quant	0.0063465	0.0116234	0.0117261	0.0106443	0.0206488	0.0303305	
	95% quant	0.0153137	0.0228446	0.0190101	0.0294107	0.0406244	0.0450477	
Panel D: Vol ^{RS}	Panel D: Vol ^{RS}							
Mean 0.0038064 0.0089922 0.0097673 0.0056961 0.0146151 0.0247391	Mean	0.0038064	0.0089922	0.0097673	0.0056961	0.0146151	0.0247391	
Std 0.0061344 0.062423 0.0125277 0.0134366 0.0152348 0.012847	Std	0.0061344	0.062423	0.0125277	0.0134366	0.0152348	0.012847	
Kurt 17.98 34649.13 22924.51 444.32 11.65 4.26	Kurt	17.98	34649.13	22924.51	444.32	11.65	4.26	
Skew 2.72 184.37 135.53 10.25 2.17 1.06	Skew	2.72	184.37	135.53	10.25	2.17	1.06	
5% quant 0 0.0034769 0 0.0068632	5% quant	0	0	0.0034769	0	0	0.0068632	
25% quant 0 0.0033214 0.0061366 0 0 0.0159229	25% quant	0	0.0033214	0.0061366	0	0	0.0159229	
50% quant 0 0.0067261 0.008711 0 0.0116377 0.0236178	50% quant	0	0.0067261	0.008711	0	0.0116377	0.0236178	
75% quant 0.0062108 0.0117933 0.0119516 0.0320555 0.0213779 0.0317143	75% quant	0.0062108	0.0117933	0.0119516	0.0320555	0.0213779	0.0317143	
95% quant 0.0159441 0.0233382 0.0192981 0.2578042 0.0420991 0.0467666	95% quant	0.0159441	0.0233382	0.0192981	0.2578042	0.0420991	0.0467666	
Panel E: Volume	Panel E: Volume							
Mean 2.28512 16.5572 47.06131 0.9122 7.3949 31.3766	Mean	2.28512	16.5572	47.06131	0.9122	7.3949	31.3766	
Std 4.93763 118.59424 28.48518 2.3133 10.7082 29.0856	Std	4.93763	118.59424	28.48518	2.3133	10.7082	29.0856	
Kurt 32.67 1.13 2.52713 148.16 6.5689 2088.77	Kurt	32.67	1.13	2.52713	148.16	6.5689	2088.77	
Skew 4.51 1.31 1.23702 7.19 2.3733 14.62	Skew	4.51	1.31	1.23702	7.19	2.3733	14.62	

(Continued)



Table 2. (Continued)

-	XAU			XAG		
	2000–2005	2005–2010	2010–2015	2000–2005	2005–2010	2010–2015
5% quant	0	0	11	0	0	3
25% quant	0	2	27	0	0	14
50% quant	0	9	44	0	3	25
75% quant	2	26	59	1	10	39
95% quant	12	57	104	5	31	89
Panel F: BAS		·		·		
Mean	0.0018539	0.0013977	0.0006002	0.0043048	0.0044053	0.0028778
Std	0.0006416	0.0006908	0.0002486	0.0011092	0.0019853	0.0305432
Kurt	263.96	504.39	15.14	733.25	6.01	4263.46
Skew	11.68	8.94	2.33	15.35	1.72	65.25
5% quant	0.0012523	0.0007244	0.0002016	0.0028531	0.0023895	0.0010045
25% quant	0.0016095	0.0009029	0.0004774	0.0040241	0.0030143	0.0014489
50% quant	0.0018152	0.0012031	0.0005766	0.0043073	0.0037125	0.002007
75% quant	0.0018972	0.001642	0.0006846	0.0045351	0.005301	0.0028531
95% quant	0.0025924	0.0025238	0.0009878	0.0060423	0.0085561	0.0050865
Obs	359,772	360,180	359,928	359,676	360,180	359,894

https://doi.org/10.1371/journal.pone.0174232.t002

returns were positively skewed compared to negative skewness in the previous two periods, indicating that the gold returns in the 2010–2015 period behaved differently to the previous periods. The SQ and GK volatility measures show that volatility increased from the first sub-sample to the second subsample, but in the final subsample the volatility is at its lowest. The RS measure, however, suggests that volatility has increased over time in each subsample



https://doi.org/10.1371/journal.pone.0174232.g003



Fig 4. Time-series graphs of the squared returns measure of volatility of the four precious metals. https://doi.org/10.1371/journal.pone.0174232.g004

period. The volume results show that the number of trades for gold has increased substantially over time, from 2.28 in the first subsample to 47.06 in the third subsample indicating the increase in trading in gold over the previous 15 years. The mean BAS has also decreased substantially over time, from 0.00185 in the 2000–2005 period to 0.000600 in the 2010–2015 period, also indicating an increase in liquidity and efficiency of the gold market. This finding is consistent with a number of other empirical studies.

The silver sub-sample results show that in the first period silver had a positive mean return, which turned negative in the middle period and increasingly negative in the final period. The 2005–2010 period has the largest standard deviation of returns, while the 2010–2015 period experiences the largest kurtosis of returns. All periods experience negative skewness with the 2005–2010 period experiencing the largest negative skewness. The SQ volatility measure suggests that the 2005–2010 subsample has the highest mean volatility, while the GK and RS measures both suggest that volatility has increased over time with the final subsample exhibiting the largest volatility. Similar to gold, the mean volume of trades of silver increases over time, from 0.91 in the 2000–2005 period to 31.38 in the 2010–2015 period indicating an increase in liquidity over time. Furthermore, the BAS has decreased over time from 0.00430 in the 2000–2005 period to 0.00288 in the 2010–2015 period, again suggesting an increase in liquidity and efficiency in the silver market.

The sub-sample platinum results are reported in Table 3, the largest mean return is in the 2000–2005 period while the other two subsamples have negative mean returns. The first period has the largest standard deviation of returns and all the returns have positive kurtosis and negative skewness, with the 2000–2005 period having the largest negative skewness. All three volatility measures suggest that the 2000–2005 period has the largest mean volatility and the 2005–2010 subsample is the least volatile period. The mean volume of platinum increases over time from 1.11 in the 2000–2005 period to 15.91 in the 2010–2015 period indicating a substantial



Table 3. Descriptive statistics for platinum and palladium over the three subsamples. 'SQ' denotes the squared returns measure of volatility, 'GK' denotes the Garman-Klass measure while 'RS' denotes the Rogers-Satchell measure.

	XPT XPD					
	2000–2005	2005–2010	2010–2015	2000–2005	2005–2010	2010-2015
Panel A: Returns						
Mean	0.0000261	-0.0002689	-0.0004081	-0.0003236	0.0001407	-0.0003292
Std	0.2316635	0.1313224	0.1325972	0.4563751	0.5106873	0.2089926
Kurt	65.16	12.4	10.22	21.24	42.34	4.9
Skew	-0.31	-0.27	-0.22	-1.3	-0.64	-0.1664
5% quant	-0.3243761	-0.2131644	-0.2161918	0	-0.835078	-0.3611549
25% quant	0	-0.0642675	-0.0650618	0	0	-0.0831324
50% quant	0	0	0	0	0	0
75% quant	0	0.065083	0.0644745	0	0	0.082306
95% quant	0.288123	0.206541	0.215728	0.508907	0.805806	0.369086
Panel B: Vol ^{SQ}						·
Mean	0.0536678	0.0172456	0.0175821	0.2082778	0.2608008	0.0436779
Std	0.4398046	0.0654449	0.0614795	1.0040702	1.7365975	0.1147294
Kurt	82256.58	5901.34	7095.85	516.42	78042.21	2210.22
Skew	216.23	59.3982271	59.76	14.96	230.06	25.4568
5% quant	0	0	0	0	0	0
25% quant	0	0.0006522	0.000581	0	0	0.0009081
50% quant	0	0.0041785	0.0041947	0	0	0.0068422
75% quant	0.0133805	0.0188734	0.018502	0	0.0474652	0.0411502
95% quant	0.2083128	0.0700132	0.0743775	1.4692834	1.2913595	0.1969263
Panel C: Vol ^{GK}						
Mean	0.0064574	0.0230374	0.0252609	0.0052386	0.0115267	0.0259776
Std	0.0121131	0.0107706	0.0125457	0.0184928	0.0230601	0.0162669
Kurt	9.75	9.16	4.06	141.37	43.15	-0.0415584
Skew	2.72	1.45	1.0734	8.48	4.76	0.5461874
5% quant	0	0.0073931	0.0076231	0	0	0.0034676
25% quant	0	0.0165241	0.0171216	0	0	0.0124797
50% quant	0	0.0221416	0.0234502	0	0	0.0244
75% quant	0.0072826	0.0284787	0.0317613	0	0.0149993	0.0374223
95% quant	0.0336807	0.041013	0.0480681	0.0312871	0.0538244	0.0541242
Panel D: Vol ^{RS}		1			1	
Mean	0.0054296	0.0247651	0.0273644	0.0015561	0.0084784	0.0276124
Std	0.0125796	0.0125911	0.014309	0.014508	0.0210822	0.0184613
Kurt	12.79	16.75	8.43	711.29	20.74	0.1865454
Skew	3.1	2.08	1.49	19.1	3.72	0.5839
5% quant	0	0.00599645	0.0070885	0	0	0
25% guant	0	0.0176513	0.0184945	0	0	0.0125471
50% guant	0	0.02397	0.0254553	0	0	0.0257088
75% guant	0	0.0307562	0.0343755	0	0	0.0406122
95% quant	0.0345248	0.0442156	0.0524275	0	0.0531628	0.0592283
Panel E: Volume				-		
Mean	1.1077	12.5458	15.9085	0.0752	0.6777	10.6456
Std	3.4527	10.8855	15.1886	0.3649	1.9821	183.6478
Kurt	242.87	10.64	4983.8	499.9	55.3419	40505.6
Skew	9.87	2.45	25.95	12.31	5.8662	200.43

(Continued)



Table 3. (Continued)

	ХРТ			XPD		
	2000–2005	2005–2010	2010–2015	2000–2005	2005-2010	2010-2015
5% quant	0	0	1	0	0	0
25% quant	0	5	7	0	0	3
50% quant	0	11	13	0	0	7
75% quant	1	16	19	0	0	13
95% quant	7	32	47	1	4	32
Panel F: BAS						
Mean	0.006409	0.0049555	0.0050733	0.0267059	0.0172727	0.0079489
Std	0.0049016	0.0049242	0.0049665	0.0084668	0.0079979	0.0069243
Kurt	17.04	151108.09	146149.84	2.8085356	6.83	76128.69
Skew	3.47	-2.76	-2.76	1.1	2.18	264.65
5% quant	0.0030817	0.0028241	0.0025684	0.0149925	0.00907803	0.0048251
25% quant	0.004008	0.0040628	0.0041728	0.0210526	0.01204822	0.0070274
50% quant	0.004761	0.0048997	0.0050234	0.0254453	0.0152091	0.0076211
75% quant	0.0059701	0.0061425	0.0063336	0.0309598	0.01988078	0.0085616
95% quant	0.0168138	0.0071136	0.0073651	0.0424328	0.0322581	0.0114811
Obs	359,727	360,180	359,902	359,606	360,180	359,902

https://doi.org/10.1371/journal.pone.0174232.t003

increase in liquidity over time. Also, the BAS decreased from 0.0064 in the 2000–2005 subsample to 0.0050 in the 2005–2010 subsample. The BAS in the final subsample is slightly higher at 0.0051, indicating that from the first subsample to the final two the BAS has decreased, consistent with an increase in liquidity and efficiency of the platinum market.

The palladium results show that the 2000–2005 and 2010–2015 periods have negative mean returns, while the 2005–2010 period has a positive mean return. The 2005–2010 period experiences the largest standard deviation of returns and all periods have positive kurtosis and negative skewness. The SQ and RS measures of volatility indicate that the 2005–2010 period has the highest mean volatility while the GK measure suggests the 2010–2015 period has the highest volatility. The mean volume of trades increases substantially over time, from 0.08 in the 2000–2005 subsample to 10.65 in the 2010–2015 subsample. The BAS has decreased over time, from 0.02670 in the 2000–2005 period to 0.00795 in the 2010–2015 period, indicating an increase in liquidity and efficiency of the palladium market.

The sub-period results show that each precious metal experienced negative mean returns in the 2010–2015 period and that the number of trades increased substantially over time. Furthermore, the trading volume in the first sub-sample period is very low for each precious metal, indicating the lack of liquidity at the 5-minute level. Therefore our results show that the behaviour of precious metals has changed substantially over time.

Intraday stylized facts

Fig 5 reports the intraday mean volume of trades at the 5-minute intervals, all four precious metals exhibit n-shaped patterns, the number of trades increases until the early afternoon GMT and then falls away. This is consistent with the opening hours of European markets (9 AM to 5 PM GMT) and North American markets (about 3 PM to 8 PM GMT), where the highest volume of trades takes place round 11 AM GMT to 5 PM GMT when both markets are open. These findings suggest the possible presence of a periodic pattern in volume, which is investigated in more detail on the subsample level.



https://doi.org/10.1371/journal.pone.0174232.g005

The intraday mean BAS at the 5-minute intervals for each precious metal are reported in Fig $\underline{6}$ and show that the mean BAS for gold and silver is fairly constant throughout the day. Both markets exhibit a small increase in the BAS around 10 PM GMT, possibly due to the daily hour closure of the markets from 9 PM GMT to 10 PM GMT. Platinum also shows a fairly constant BAS throughout the day with some very small fluctuations around 10 PM GMT. Palladium however exhibits some periodicity, with the BAS largest from midnight GMT to 6 AM GMT, which then falls and stays fairly constant until the end of the day, which could be the results of the opening (and anticipation) of European markets. Fig 7 reports the intraday volatility through the three volatility measures previously discussed and shows that the volatility for gold is fairly constant up to 12 PM GMT and then increases slightly until 2 PM GMT. After this point, volatility decreases and levels off to the end of the day. Silver's volatility is fairly constant throughout the day, with again a small increase around 12 PM GMT which continues until 2 PM GMT. The GK and RS volatility for platinum and palladium are very similar and fairly constant throughout the day, while the SQ measure of volatility is little more variable with a few sharp jumps at various points of the day although there is no clear periodicity.

Dynamic intraday stylized facts

As we have seen in Tables 2 and 3, the behaviour of the four precious metals has changed substantially over time and so their intraday behaviour may also change, depending on the sub period examined. Therefore we also study the dynamic intraday stylized facts in three subsamples to examine whether the behaviour of the precious metals markets change depending on the time period examined.

Fig 8 shows the intraday volume of trades over the three subsamples and shows that each subsample experiences daily periodicity, albeit at different magnitudes. For instance, the









https://doi.org/10.1371/journal.pone.0174232.g007



volume of trades of gold increases throughout the day and then decreases from around 5 PM GMT, similar to what was found in Fig 5. For all four precious metals, the increase in the volume of trades is much larger from the second to the third subsample than the first to the second subsample, indicating a much larger increase in trading of precious metals after 2010. The intraday BAS over the three subsamples is reported in Fig 9 which, similar to the intraday BAS over the full sample, shows very little pattern throughout the day as the BAS seems to remain fairly constant in each subsample period. As expected from our previous analysis, the BAS of each precious metal market. Fig 10 presents the intraday squared returns measure of volatility over the three subsamples and for gold and silver, the patterns are very similar. For platinum, we find that the volatility during the first subsample is much greater throughout the day than for the most recent subsamples while we find that the most recent subsamples The other measures of volatility show similar patterns and are not reported to conserve space but available upon request.

Correlation

A well-known stylised fact in finance is that stock index returns are negatively correlated with changes in volatility [26] and that the relationship is even more pronounced in falling than in rising markets [43]. There has been much evidence of this relationship in stock market indices but little in precious metals, especially at high-frequency. To examine the lead-lag relationship between returns and volatility of returns, we calculate the correlation coefficient of the precious metals returns at the 5-minute internal *t* with VSQ and VGK in 5-minutes internal t + j, where $j \in \{-500, \ldots, 500\}$. Calculations are based on all *t* during the total sample period. The RS



https://doi.org/10.1371/journal.pone.0174232.g009

graphs are almost identical to those of the GK and are not included but are available upon request.

Fig 11 shows the correlation coefficient is near zero for lagged SQ volatility (j < 0) for all precious metals. Thus, precious metals return does not seem to be systematically related to the preceding SQ volatility. However, we find a significantly negative correlation for all four precious metals returns not only with contemporaneous volatility (j = 0), but also the volatility in the next few 5-minute periods. This observation supports the hypothesis that volatility is adjusted to changes in the index level. We also study the GK volatility measure interaction with returns in Fig 12, which shows similar results to Fig 11, with lagged volatility generating near zero coefficients and some significant negative correlation coefficients. Again, this is compatible with a return-driven effect. We also study the correlation between volatility and returns for our three subsamples and find them to be almost identical to ones reported in Figs 11 and 12 and are available upon request. However, correlations computed at lags > 1 could be due to the correlation at lag j = 1. This is why it is necessary to identify causality and the number of lagged returns which have an impact on contemporaneous volatility.

Vector autoregression model

To explore the casual relationships between volatility and returns of high-frequency precious metal data, a vector autoregression (VAR) model is estimated. Granger causality tests are then conducted to determine the direction of the causal linkages.

We consider a VAR model of order *p* in which;

$$y_t = c + \sum_{t=1}^p \phi_i y_{t-1} + \varepsilon_t \tag{6}$$



Fig 10. The mean squared returns measure of volatility for each 5-minute period over the three subsamples for the four precious metals.



https://doi.org/10.1371/journal.pone.0174232.g011



Fig 12. The correlation between returns and volatility, measured by the Garman and Klass (1980) measure over the full sample period for different lead and lag intervals.

where y_t is a $(n \times 1)$ vector of endogenous variables, $c = (c_1, \ldots, c_n)$ is the $(n \times 1)$ intercept vector of the VAR, ϕ_i is the *i*th $(n \times n)$ matrix of autoregressive coefficients for $i = 1, 2, \ldots, p$, and $\varepsilon_t = (\varepsilon_{1t}, \ldots, \varepsilon_{nt})$ is the $(n \times 1)$ generalization of a white noise process. We model the return volatility relationships across the four precious metals where the models are estimated up to a maximum lag of 12 and the optimal lag length is selected by using the Akaike information criterion (AIC), similar to [44].

After estimating the VAR model, the Granger causality test is conducted, this is a popular way to test if there is any temporal statistical relationship with a predictive value between the two time series [45]. This test indicates any possible short-run predictive interrelationships among the series. When 'X Granger causes Y', it does not mean that Y is the effect or the result of X. Granger causality measures precedence and information content and thus 'causality' is defined in terms of predictability, hence variable X causes variable Y if present Y can be better predicted by using past values of X than by not doing so, with respect to a given information set that includes X and Y.

Table 4 summaries the results of the Granger causality test for the full sample period as well as the three subsample periods for the return-driven relationship in Panel A and the volatilitydriven relationship in Panel B. The results clearly show strong evidence of a return-driven relationship across all sample periods and all three measures of volatility for platinum and palladium. For gold we find significant evidence of a return-driven relationship at the 5% level for all measures and sample periods except the GK and RS measures in the 2005–2010 period, where the return-driven relationship is only significant at the 7% level. For silver, we find significant evidence of a return-driven relationship for all sample periods for all SQ and RS volatility measures but find insignificant evidence for the GK measure in the 2000–2015, 2000– 2005 and 2010–2015 periods. We also find significant evidence of a volatility-driven relationship since all p-values are significant at the 5% level. That means that past volatility does add



	2000–2015			2000–2005			2005–2010			2010-2015		
	SQ	GK	RS	SQ	GK	RS	SQ	GK	RS	SQ	GK	RS
Panel A	Return-driven re	lationship										
XAU	0	0.02	0.02	0	0	0	0	0.07	0.07	0	0.04	0.01
XAG	0	0.72	0	0	0.12	0	0	0.03	0.01	0	0.78	0
XPT	0	0	0	0	0	0	0	0	0	0.01	0	0
XPD	0	0	0	0	0	0	0	0	0	0	0	0
Panel B	: Volatility-driven i	elationshi	C									
XAU	0	0	0	0	0	0	0	0.04	0.05	0	0	0
XAG	0	0	0	0	0	0	0	0	0	0	0	0
XPT	0	0	0	0	0	0	0	0	0	0	0	0
XPD	0	0	0	0	0	0	0	0	0	0	0	0

Table 4. The Granger causality test result p-values for the full sample and three subsamples of the return-volatility relationships. 'SQ' denotes the squared returns measure of volatility, 'GK' denotes the Garman-Klass measure and 'RS' denotes the Rogers-Satchell measure of volatility.

https://doi.org/10.1371/journal.pone.0174232.t004

significant explanatory power of past returns in explaining current returns. This relationship is consistent across sample periods and across measures for volatility. Therefore we provide evidence of a bi-lateral relationship between returns and volatility of precious metals, in that returns and volatility both have strong explanatory power in explaining current volatility and current returns.

Discussion and conclusions

This study investigates the intraday periodicity, correlation and volatility interaction of returns, volatility, volume and BAS that occur in 5-minute data for the key precious metals: gold, silver, platinum and palladium. We study the intraday periodicity as well as the relation-ship between returns and volatility from 2000 to 2015, as well as in three subsamples to determine how the precious metals stylized facts have developed over time. These precious metals are some of the most traded assets worldwide and they also play an important role for investors as well as comprising an important asset for central banks. Given the increased attention precious metals have received in the literature, the intraday dynamics are of great interest.

Initially, we show that the volume of trades of precious metals has increased substantially over the last 15 years' while the bid-ask spread has decreased indicating the increase in efficiency and liquidity of precious metal markets. We also show strong evidence of intraday periodicity of precious metals volume of trades and volatility. The intraday volume has increased over time, while the intraday bid-ask spread has decreased over time. The narrowing of bid-ask spreads and increased trading volume could partially be attributed to the global financial crisis of 2007–2009 and the subsequent European sovereign debt crisis since market participants may have chosen to gold as a safe haven or risk-hedging tool during this period (see [46] for more details). We also study the interaction between volatility and returns of each precious metal and our correlation analysis shows that returns are negatively correlated with the contemporaneous volatility and the previous 5-minute volatility. Furthermore, we find bi-directional Granger causality between volatility and returns suggesting that past volatility (returns) offers significant explanatory power in explaining current returns (volatility).

Author Contributions

Conceptualization: JB FM BL AU MP.

Data curation: MP AU.

Formal analysis: JB FM BL AU MP.

Investigation: JB FM BL AU MP.

Methodology: JB FM BL AU MP.

Resources: MP AU.

Software: AU.

Supervision: JB FM BL AU MP.

Validation: JB FM BL AU MP.

Writing - original draft: JB FM BL AU MP.

Writing – review & editing: JB FM BL AU MP.

References

- World Federation of Exchanges 2011 Annual Report. http://www.world-exchanges.org/files/statistics/ pdf/2011_WFE_AR.pdf
- 2. Report on global foreign exchange market activity in 2010.http://www.bis.org/publ/rpfxf10t.pdf
- 3. Hauptfleisch M., Putniņš T. J., & Lucey B. (2016). Who sets the price of gold? London or New York. Journal of Futures Markets, 36(6), 564–586.
- 4. Lockwood L.J., Linn S. C. (1990). An examination of stock market return volatility during overnight and intraday periods, 1964–1989. *Journal of Finance*, 45, 591–601.
- McInish T. H., Wood R. A., (1992). An analysis of intraday patterns in bid/ask spreads for NYSE stocks. Journal of Finance, 47(2), 753–764.
- Evans K. P., Speight A. E. H. (2010). Intraday periodicity, calendar and announcement effects in Euro exchange rate volatility. *Research in International Business and Finance*, 24, 82–101.
- Heston S. L., Korajczyk R. A., Sadka R. (2010). Intraday patterns in the cross-section of stock returns. *The Journal of Finance*, 65, 1369–1408.
- 8. Broussard J. P., Nikiforov A. (2014). Intraday periodicity in algorithmic trading. *Journal of International Financial Markets, Institutions and Money*, 30, 196–204.
- Baillie R. T., Bollerslev T. (1991). Intra Day and Inter Market Volatility in Foreign Exchange Rates. Review of Economic Studies, 58, 565–585.
- Ranaldo A. (2009). Segmentation and Time-of-Day Patterns in Foreign Exchange Markets. *Journal of Banking and Finance*, 33, 2199–2206.
- Breedon F., Ranaldo A. (2013). Intraday Patterns in FX Returns and Order Flow. Journal of Money, Credit and Banking, 45(5), 953–965.
- Chelley-Steeley P., Park K. (2011). Intraday patterns in London listed Exchange Traded Funds. International Review of Financial Analysis, 20(5), 244–251.
- 13. McInish T. H., Wood R. A. (1990a). An analysis of transactions data for the Toronto Stock Exchange. *Journal of Banking and Finance*, 14, 441–458.
- Brock W. A., Kleidon A. W. (1992). Periodic market closure and trading volume: A model of intra-day bids and asks. *Journal of Economic Dynamics and Control*, 16, 451–489.
- Hamao Y., Hasbrouck J. (1993). Securities trading in the absence of dealers: Trades and quotes on the Tokyo Stock Exchange. *The Review of Financial Studies*, 8, 849–878.
- 16. Ellul, A., Shin, H. S., Tonks, I. (2002). Towards deep and liquid markets: Lessons from open and close at the London Stock Exchange. LSE Financial Markets Group working Paper.
- Cai X., Hudson R., Keasey K. (2004). Intraday bid-ask spreads, trading volume and volatility: Recent empirical evidence from the London Stock Exchange. *Journal of Business Finance and Accounting*, 31, 647–676.
- Naik, N., Yadav, P. K. (1999). The effects of market reform on trading costs of public investors: Evidence from the London Stock Exchange. Working paper, London Business School.
- Wood A. R., McInish H. T., Ord K. (1985). An investigation of transactions data for NYSE stocks. *Journal of Finance*, 40, 723–739.

- McInish T. H., Wood R. A. (1990b). A transaction data analysis of the variability of common stock returns during 1980–1984. *Journal of Banking and Finance*, 14, 99–112.
- Madhavan A., Richardson M., Roomans M. (1997). Why do security prices change? A transactions level analysis of NYSE stocks. *Review of Financial Studies*, 10, 1035–1064.
- Caporin M., Ranaldo A., Velo G. (2015). Precious metals under the microscope: a high-frequency analysis. *Quantitative Finance*, 15(5), 743–759.
- Cai J., Cheung Y., Wong M. C. S. (2001). What moves the gold market? *Journal of Futures Markets*, 21, 257–278.
- 24. Baillie R. T., Han Y. Myers R. J., Song J. (2007). Long-memory models for daily and high-frequency commodity future markets. *Journal of Futures Markets*, 27(7), 643–668.
- Khalifa A. A. A., Miao H., Ramchander S. (2011). Return distribution and volatility forecasting in metal futures markets: Evidence from gold, silver and copper. *Journal of Futures Markets*, 31(1), 55–80.
- Black, F. (1976). Studies of stock price volatility changes, Proceedings of the meetings of the American Statistical Association, Business and Economics Section, Chicago, 177–181.
- 27. Bekaert G., Wu G. (2000). Asymmetric volatility and risk in equity markets. *Review of Financial Studies*, 13, 1–42.
- Bollerslev T., Litvinova J., Tauchen G. (2006). Leverage and volatility feedback effects in high-frequency data. *Journal of Financial Econometrics*, 4, 353–384.
- 29. Dennis P., Mayhew S., Stivers C. (2006). Stock returns, implied volatility innovations, and the asymmetric volatility phenomenon. *Journal of Financial and Quantitative Analysis*, 41, 381–406.
- **30.** Giot P. (2005). On the relationships between implied volatility and stock index returns. *Journal of Portfolio Management*, 26, 12–17.
- **31.** Hafner R., Wallmeier M. (2007). Volatility as an asset class: European evidence. *European Journal of Finance*, 1, 1–27.
- Chai E. F. L., Lee A. D., & Wang J. (2015). Global information distribution in the gold OTC markets. International Review of Financial Analysis, 41, 206–217.
- Edwards A. K., Harris L. E., & Piwowar M. S. (2007). Corporate bond market transaction costs and transparency. *Journal of Finance*, 62(3), 1421–1451.
- Loon Y. C., & Zhong Z. K. (2016). Does Dodd-Frank affect OTC transaction costs and liquidity? evidence from real-time CDS trade reports. *Journal of Financial Economics*, 119(3), 645–672.
- 35. Murray S. (2011). Loco London Liquidity Survey. The Alchemist, 63, 9–10.
- Goodhart C. A. E., O'Hara M. (1997). High frequency data in financial markets: Issues and applications. Journal of Empirical Finance, 4, 73–114.
- Anderson T. G., Bollerslev T., Cai J. (2000). Intraday and interday volatility in the Japanese stock market. *Journal of International Financial Markets, Institutions and Money*, 10, 107–130.
- Hol, R., Koopman, J. (2002). Stock index volatility forecasting with high frequency data. Tinbergen Institute Discussion Papers. 02-068/4.
- Koutmos G., Martin A. D. (2011). Currency bid-ask spread dynamics and the Asian crisis: Evidence across currency regimes. *Journal of International Money and Finance*, 30, 62–73.
- Garman M., Klass M. (1980). On the estimation of security price volatiles from historical data. *Journal of Business*, 53, 67–78.
- 41. Rogers L., Satchell S. (1991). Estimating variance from high, low, and closing prices. *Annuals of Applied Probabilities*, 1, 500, 512.
- Rogers L., Satchell S., Yoon Y. (1994). Estimating the volatility of stock prices: a comparison of methods that use high and low prices. *Applied Financial Economics*, 4, 241–247.
- Figlewski, S., Wang, X. (2000). Is the Leverage Effect still a Leverage Effect? Working Paper Series 00–37 (New York University).
- Jain A., Biswal P. C., Ghosh S. (2016). Volatility-volume causality across single stock spot-futures markets in India. *Applied Economics*, 48(34), 3228–3243.
- Granger C. W. J. (1969). Investigating causal relations by econometric models and cross-spectral methods. *Econometrica*, 37(3), 424–438.
- Wang G. J., Xie C., Jiang Z. Q., Stanley H. E. (2016). Extreme risk spillover effects in world gold markets and the global financial crisis. *International Review of Economics & Finance*, 46, 55–77.